

## NEWTONS LAWS OF MOTION

1.

$$\text{Change} = mv - (-mv)$$

$$= 0.1\text{kg} \times 20 - (-0.1 \times 0.1 \times 30) [1\text{m}]$$

$$= 5\text{Kgm/s} [1\text{m}]$$

2.

(a) (i) any mention of force or weight ignore mass C1  
Force to left > force to right )

OR resultant force ) any 1 A1

OR unbalanced force )

OR weight > friction )

(ii) to overcome/compensate for friction/resistance B1

(b) 2/2.5 or 4/5 etc. or  $F/a$  or  $F = ma$  C1

0.8 kg A1

(c) 0.7/0.8 e.c.f. from (b) B1

0.875 (m/s<sup>2</sup>) e.c.f. from (b) could be scored on table (no unit needed) B1

(d) (i)  $v = at$  or  $0.5 \times 1.2$  C1

0.6 m/s A1

(ii) any velocity  $\times$  time or speed  $\times$  time C1

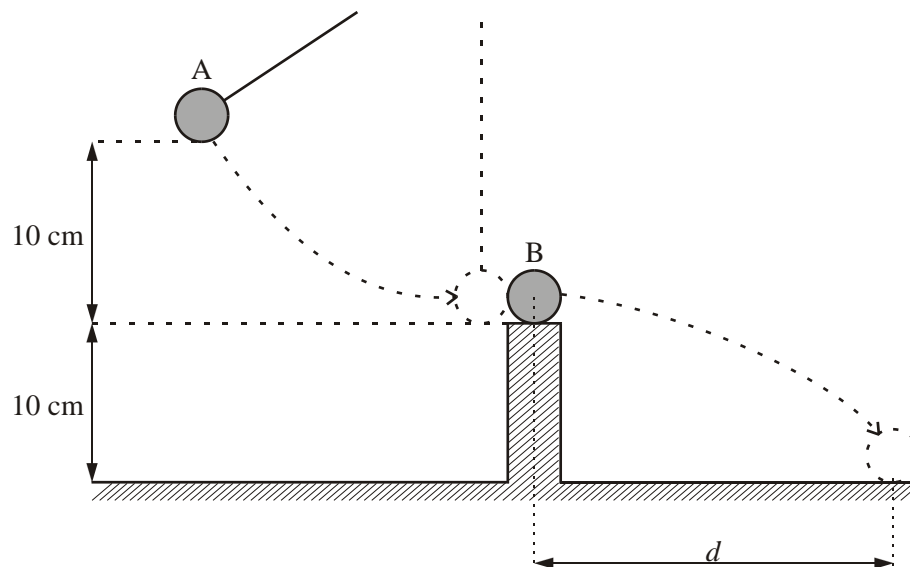
0.36 m c.a.o. (note: 0.72 m gets C1, A0) A1 [11]

3.

A

4.

The diagram illustrates an elastic collision between two spheres, A and B, of equal mass.



Sphere A is tied to the end of a long vertical thread and pulled to one side until it has risen a distance of 10 cm. It is then released and comes to rest when it strikes the sphere B

which is resting on a smooth flat support.

Sphere B travels a horizontal distance  $d$  before it hits the ground after falling 10 cm.

Calculate the speed of A as it strikes B.

$$\text{Gain of kinetic energy} = \text{loss in potential energy} \quad (1)$$

$$v = \sqrt{2gh} \quad (1)$$

$$\sqrt{2 \times (9.8 \text{ m s}^{-2}) \times (0.10 \text{ m})} \quad (1)$$

$$\text{Speed} = 1.4 \text{ m s}^{-1} \quad (1)$$

(4 marks)

How long does B take to fall 10cm?

$$t = \sqrt{2s/g} \quad (1)$$

$$= \sqrt{2 \times (0.10 \text{ m}) / (9.8 \text{ m s}^{-2})} \quad (1)$$

$$\text{Time} = 0.14 \text{ s} \quad (1)$$

(3 marks)

What is the speed of B just after the collision?

$$1.4 \text{ m s}^{-1} \quad (1)$$

(1 mark)

Calculate the distance  $d$

$$\text{Distance} = \text{speed} \times \text{time} = (1.4 \text{ ms}^{-1}) (0.14\text{s}) \quad (1)$$

$$\text{Distance} = 0.20 \text{ m} \quad (1)$$

(2 marks)

Explain briefly why B drops a distance of 10 cm much more quickly than A.

B is in free fall (1)

while the downwards acceleration of A is inhibited by the upward tension in the string (1)

(2 marks)

[Total 12 marks]

5.

(a) (i) momentum is mass  $\times$  velocity; 1

(ii) impulse is force  $\times$  time / change in momentum; 1

*In each case allow an equation, with symbols explained.*

(b) (i)  $Dp = 450 (18 - 13);$  1

$$= 2250 \text{ kg m s}^{-1}$$

(ii) idea of equating  $Dp$  to change in momentum of water;

$$\frac{2250}{19}$$

$$m = \frac{2250}{19} = 118 \text{ kg } (\approx 120\text{kg});$$

2

$$\begin{aligned}
 \text{(iii) time of trolley in tank} &= \frac{9.3}{15.5} = 0.60 \text{ s;} \\
 a &= \frac{(18-13)}{0.60} \quad \text{or} \quad \text{force} = \frac{2250}{0.60} (= 3750 \text{ N}); \\
 a &= 8.3 \text{ m s}^{-2} \quad a = \frac{3750}{450} = 8.3 \text{ m s}^{-2};
 \end{aligned}$$

$$\begin{aligned}
 &\text{or} \\
 v^2 &= u + 2as \\
 a &= \frac{13^2 - 18^2}{2 \times 9.3}; \\
 a &= 8.3 \text{ m s}^{-2};
 \end{aligned}$$

$$\begin{aligned}
 \text{(c) (i)} \quad E_K &= \frac{1}{2}mv^2; \\
 &= \frac{1}{2} \times 450 \times (18^2 - 13^2); \\
 &= 35000 \text{ J};
 \end{aligned}$$

$$\begin{aligned}
 \text{(ii)} \quad E_K &= \frac{1}{2} \times 118 \times 19^2 \\
 &= 21000 \text{ J; (allow 22 000 J for use of } m=120 \text{ kg)}
 \end{aligned}$$

- (d) some water will be thrown “sideways”;  
 this will account for the difference in the kinetic energies;  
 this will not have any momentum in the forward direction / equal masses of water to left and right;

[15]

6.

- (a) before and after collision there are no forces acting on the objects;  
 from Newton 3 when the two bodies are in contact the forces that they exert on each other are equal and opposite / OWTTE;  
 therefore, the net force on the two balls is always zero;  
 therefore, there is no change in momentum (of the objects) / momentum is conserved;

or

Accept an argument based on change in momentum of each individual object.

eg

from Newton 3  $F_{12} = -F_{21}$ ; (accept statement in words)

$$F_{12} = \frac{\Delta p_1}{\Delta t} \text{ and } F_{21} = \frac{\Delta p_2}{\Delta t};$$

$$\frac{\Delta p_1}{\Delta t} = -\frac{\Delta p_2}{\Delta t};$$

therefore,  $\Delta p_1 + \Delta p_2 = 0$ ; 4

- (b) the blades exert a force on the air and by Newton's third law the air exerts an equal and opposite force on the blades / air has change in momentum downwards giving rise to a force and from Newton 3 there will a force upwards;  
if this force equals the weight of the helicopter;  
the net vertical force on the helicopter will be zero / *OWTTE*; 3

(c)  $\text{area} = \pi r^2$ ;  
 $= 1.5 \text{ m}^2$  1

(d) (i) volume of air per second =  $1.5 \times 4.0 (\text{m}^3 \text{s}^{-1})$ ;  
mass = volume  $\times$  density =  $(1.2 \times 1.5 \times 4.0) = 7.2 \text{ kg s}^{-1}$ ; 2  
*No unit error for 7.2 kg.*

(ii) momentum per second =  $(7.2 \times 4.0) = 29 \text{ N}$ ; 1

(e) 29 N; 1

(f) recognize that the force on the blades =  $Mg$ ;  
to give 3.0 kg; 2

7.

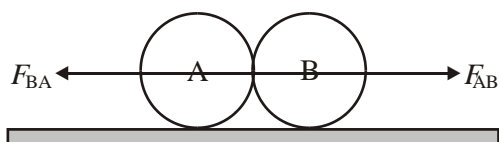
- (a) when two bodies A and B interact, the force that A exerts on B is equal and opposite to the force that B exerts on A;  
or  
when a force acts on a body an equal and opposite force acts on another body somewhere in the universe; 1 max

Award [0] for "action and reaction are equal and opposite"  
unless they explain what is meant by the terms.

- (b) if the net external force acting on a system is zero;  
then the total momentum of the system is constant (or in any one direction, is constant); 2

To achieve [2] answers should mention forces and should show what is meant by conserved. Award [1 max] for a definition such as "for a system of colliding bodies, the momentum is constant" and [0] for "a system of colliding bodies, momentum is conserved".

- (c)



arrows of equal length;  
 acting through centre of spheres;  
 correct labelling consistent with correct direction;

3

- (d) (i) Ball B:  
 change in momentum =  $Mv_B$ ;  
 hence  $F_{AB}\Delta t = Mv_B$ ; 2
- (ii) Ball A:  
 change in momentum =  $M(v_A - V)$ ;  
 hence from Newton 2,  $F_{BA}\Delta t = M(v_A - V)$ ; 2

- (e) from Newton 3,  $F_{AB} + F_{BA} = 0$ , or  $F_{AB} = -F_{BA}$ ;  
 therefore  $-M(v_A - V) = Mv_B$ ;  
 therefore  $MV = Mv_B + Mv_A$ ;  
 that is, momentum before equals momentum after collision such that the  
 net change in momentum is zero (unchanged) / OWTTE; 4

Some statement is required to get the fourth mark ie an  
 interpretation of the maths result.

- (f) from conservation of momentum  $V = v_B + v_A$ ;  
 from conservation of energy  $V^2 = v_B^2 + v_A^2$ ;  
 if  $v_A = 0$ , then both these show that  $v_B = V$ ;  
 or  
 from conservation of momentum  $V = v_B + v_A$ ;  
 from conservation of energy  $V^2 = v_B^2 + v_A^2$ ;  
 so,  $V^2 = (v_B + v_A)^2 = v_B^2 + v_A^2 + 2v_Av_B$  therefore  $v_A$  has to be zero; 3 max

Answers must show that effectively, the only way that both  
 momentum and energy conservation can be satisfied is that  
 ball A comes to rest and ball B moves off with speed  $V$ .

[17]