

FORM FOUR TERM ONE EXAM 2017

MATHEMATICS 121/1 MARKING SCHEME

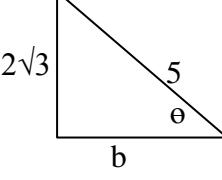
SCHOOLS NET KENYA

Osiligi House, Opposite KCB, Ground Floor
Off Magadi Road, Ongata Rongai | Tel: 0711 88 22 27
E-mail:infosnkenya@gmail.com | Website: www.schoolsnetworkkenya.com

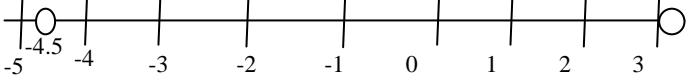
MATHEMATICS 121/1

MARKING SCHEME

1	$\frac{0.4 \div 0.22 - 1.10}{0.125 + 0.251}$ $\frac{1.818 - 1.10}{0.125 + 0.251}$ $\frac{0.718}{0.376}$ <p>=1.910</p>	M1 M1 A1	For ✓ removal of brackets and division
2	$5148 = 2^2 \times 3^2 \times 11 \times 13$ $6048 = 2^2 \times 3^2 \times 13^2$ $\frac{2^2 \times 3^2 \times 11 \times 13^2}{2^2 \times 3^2 \times 13^2}$ $\frac{2^4 \times 3^4 \times 11^2 \times 13^2}{2 \times 3 \times 13}$ $2^3 \times 3^3 \times 11^2 \times 13$	B1 M1 A1	
3	<p>Total sales $\frac{97.5}{100} \times 385,000$</p> <p>commission= 375,375</p> $\frac{3}{100}x 150,000 + \frac{1.5}{100} (375,375 - 150,00)$ $4,500 + 3,380.60$ 7880.60	M1 M1 A1 4	
4.	$\frac{4-x}{2x+1} = \frac{1}{7}$ $28 - 7x = 2x + 1$ $27 = 9x$ $x = 3$ <p>B $-1,3$ (x,y)</p> $\frac{y-3}{x+1} = -7$ $y - 3 = -7x - 7$ $y = -7x - 4$	M1 A1 M1 A1 4	
5.	$25^x \cdot 25^{-1} + 5^{2x} = 130$		Alt

	$5^{2x} \cdot \frac{1}{25} + 1 = 130$ $5^{2x} = 130 \times \frac{25}{26}$ $5^{2x} = 5^3$ $x = \frac{3}{2}$	M1 M1 A1	Let $y = 5^{2x}$ $y \cdot \frac{1}{25} + y = 130$ $y + 25y = 130 \times 25$ $y = \frac{130 + 25}{26}$ $= 125$ $5^3 = 5^{2x}$ $x = \frac{3}{2}$
6	<i>Gain in speed</i> $72 - 56 \text{ km/h}$ $= 16 \text{ km/h}$ <i>distance in 54 sec</i> $\frac{16 \times 1000 \times 54}{60 \times 60}$ $= 240$ <i>length of second train</i> $240 - 100$ $= 140 \text{ m}$	B1 M1 A1 3	
7.	 $(2\sqrt{3})^2 + b^2 = 5^2$ $b^2 = 25 - 12$ $b = \sqrt{13}$ $\tan \theta = \frac{2\sqrt{3}}{\sqrt{13}}$	M1 A1 2	
8.	<i>no of girls</i> $\frac{2}{7}x \times 35 = 10$ <i>boys</i> $45 - 10 = 35$ $\frac{10+x}{35} = \frac{4}{5}$ $50 + 5x = 140$ $5x = 140 - 50 = 90$ $x = 18$	M1 M1 A1	<i>no. of girls</i>

9	$\frac{2}{x-2} - \frac{1}{x+5} = \frac{2}{x+1}$ $\frac{2(x+5) - 1(x-2)}{(x-2)(x+5)} = \frac{2}{x+1}$ $\frac{2x+10-x+2}{(x-2)(x+5)} = \frac{2}{x+1}$ $\frac{x+12}{x-2 \quad x+5} = \frac{2}{x+1}$ $\frac{2x+10-x+2}{(x-2)(x+5)} = \frac{2}{x+1}$ $x+1 \quad x+12 = 2(x-2)(x+5)$ $x^2 + 13x + 12 = 2x^2 + 6x - 10$ $x^2 - 7x - 22 = 0$ $x = \frac{7 \pm \sqrt{49+88}}{2}$ $= \frac{7 \pm \sqrt{137}}{2}$	M1 A1 M1 ✓ attempt to solve A1 4 Both values
10	$\text{longer side} = x$ $\text{shorter side} = x-4$ $\frac{1}{2}x(x+x-4) = 99$ $x^2 - 11x + 9x - 99 = 0$ $x(x-11) + 9(x-11) = 0$ $x+9(x-11) = 0$ $x = 11 \text{ or } x = -9$ $\text{longer side} = 11$ $\text{shorter side} = 7$	B1 formation of the expression M1 M1 ✓attempt to solve quadratic exp A1 4 both ✓
11	$\frac{2x^2 - 3xy - 2y^2}{9x^2 - y^2} \times \frac{3x + y}{2x + y}$ $\frac{2x^2 - 4xy + xy - 2y^2}{3x - y(3x + y)} \times \frac{3x + y}{2x - y}$ $\frac{2x(x-2y) + y(x-2y)}{(3x-y)(3x+y)} \times \frac{3x + y}{2x - y}$ $\frac{(2x+y)(x-2y)}{3x - y(3x+y)} \times \frac{3x + y}{(2x+y)}$ $\frac{x-2y}{(3x-y)}$	M1 Factorization M1 A1 3
12	$\log A = \log K + B \log h$	

	$\log k = -1.301$ $k = 0.0978$ $\log h = \frac{1.301}{4.322} = 0.3010$ $h = 2.000$	B1 M1 A1 03	
13	$\frac{1}{3}x + 2 < x + 5$ $-3 < \frac{2}{3}x$ $-9 < 2x$ $-4.5 < x$ $x + 5 < 3x - 1$ $6 < 2x$ $3 < x$ 	B1 B1 B1 B1 03	
14	$< DFE 180 - 70 = 110$ $< FBC = 25^\circ$ $< ADF = 135^\circ$ $< ABF = 135^\circ - 25^\circ$ $= 110^\circ$	B1 B1 2	
15	$\log_2 x + \log_x 2 = 2$ $\log_2 x + \frac{1}{\log_2 x} = 2$ $(\log_2 x)^2 + 1 = 2\log_2 x^2$ $(\log_2 x)^2 - 2\log_2 x^2 + 1 = 0$ let $\log_2 x = y$ $y^2 - 2y + 1 = 0$ $y^2 - y - y + 1 = 0$ $y(y-1) - 1(y-1) = 0$ $y-1 - y+1 = 0$ $y = 1$ $\log_2 x = \log_2 2$ $x = 2$	M1 M1 A1 B1 4	\checkmark change to same logs

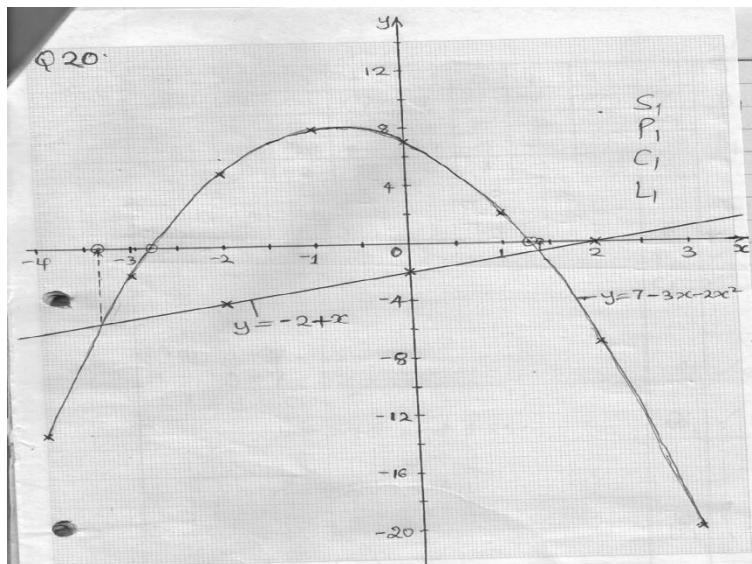
16.	$\begin{array}{rcl} \frac{a}{b} + \frac{o}{1} & = & -2 \\ b & = & 3 \end{array}$ $\begin{array}{rcl} a & = & -2 \\ b & = & 3 \\ \hline -2 & & 0 \\ 2 & & 1 \\ \hline & & -2 \end{array}$ $\begin{array}{rcl} -2 & + & \frac{c}{d} = \frac{4}{-1} \\ 2 & & d \end{array}$ $\begin{array}{rcl} c & = & 4 \\ d & = & -1 \\ \hline 6 & & -2 \\ -3 & & \\ \hline B(6, -3) & & \end{array}$		B1 B1 2
17.	$\text{area of front and back walls}$ $6.3 \times 3.2 \times 2$ $= 40.32 \text{m}^2$ $\text{area of side walls } 4.5 \times 3.2 \times 2$ $= 28.8 \text{m}^2$ $\text{area of the floor } 6.3 \times 4.5$ $= 28.35 \text{m}^2$ $\text{total area of floor and walls}$ $= 40.32 + 28.8 + 28.35$ $= 97.47 \text{m}^2$ $= \text{area of door is } 1.85 \times 0.8 = 1.48 \text{m}^2$ $\text{area of the window} = 1.5 \times 0.7 \times 4 = 4.2$ $\text{total area cemented} = 1.48 + 4.2$ $= 5.68 \text{m}^2$ $\text{area to be cemented}$ $= 97.47 - 5.68$ $= 91.79$ <p>(b)</p> $\text{cost of cementing materials} = 91.79 \times 500$ $= \text{sh. } 45900$ <p>(c)</p> $\text{cost of labour} = 20\% \times 45900$ $= 9,180$ $\text{total cost of cementing}$ $= 45900 + 9180$ $= 55080$		M1 M1 A1 M1 A1 A1 M1 A1 M1 M1 A1 M1 A1 10
18.	<p>(a)</p> $\text{angle } STQ = 28^\circ$ $\text{angles in the alt. segment}$ <p>(b)</p>	B1 B1	

	<p>(c)</p> $TQU = \frac{180 - 54}{2} = 63^\circ$ <p>base angles of isco Δ</p> $\angle TQS = 180 - 28 + 54 + 63 = 35^\circ$ <p>opp angles of cyclic quad add to 180°</p> <p>(d) reflex $\angle UOQ = 360 - 2 \cdot 54^\circ = 252^\circ$</p> <p>angles at the center = twice angle at the circum. /angles at a point</p> <p>(e) $\angle TQR = 54 + 63 = 117^\circ$ angle in the alt se</p>	B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 10
19	<p>(a)</p> $y = b + ax - x^3$ $\frac{dy}{dx} = a - 3x^2$ <p>turning pt $a - 3x^2 = 0$ $a = 3(2)^2 = 12$</p> $g = b + 12 \cdot 2 - (2)^3 = b + 24 - 8 = b + 16$ $9 = b + 16 \Rightarrow b = 9 - 16 = -7$ <p>(b) $\frac{dy}{dx} (a - 3x^2) = -6x$</p> <p>(c) maximum</p> $y = -7$ $(0, -7)$ $f = 12 - 3x^2$ <p>gradient = 12</p> $x, y = 0, -7$ $= \frac{y + 7}{x} = 12$ $= y - 12x + 7 = 0$	B1 B1 m1 A1 M1 A1 B1 M1 B1 A1 10

20

x	-4	-3	-2	-1	0	1	2	3
7	7	7	7	7	7	7	7	7
$-3x$	12	9	6	3	0	-3	-6	-9
$-2x^2$	-32	-18	-8	-2	0	-2	-8	-18
y	-13	-2	5	8	7	2	-7	-20

(b) On the graph paper



(c)(i)

$$\begin{aligned}
 y &= 7 - 3x - 2x^2 \\
 0 &= 7 - 3x - 2x^2 \\
 y &= 0 \\
 x &= 2.75 \text{ and } 1.25
 \end{aligned}$$

(ii)

$$\begin{aligned}
 y &= 7 - 3x - 2x^2 \\
 0 &= 9 + 4x + 2x^2 \\
 y &= -2 + x
 \end{aligned}$$

x	-2	0	2
y	-4	-2	0

$$x = -3.35, 1.4$$

B1

B1

S1 ✓

P1 ✓

C1 ✓

B1 ✓ evidence on the graph

B1 ✓ both correct

B1 ✓ equation

B1 ✓ both correct

10

21

(i) $PQ = q - p$

$$ii \ OR = p + \frac{2}{3}q - p$$

$$p + \frac{2}{3}q - \frac{2}{3}p$$

$$\frac{1}{3}p + \frac{2}{3}q$$

$$iii \ -\frac{3}{4}p + q$$

$$b \ ST = m \ q - \frac{3}{4}p$$

$$OT = n \ \frac{1}{3}p + \frac{2}{3}q$$

$$OT = os + st$$

$$= \frac{3}{4}p + m \ q - \frac{3}{4}p$$

$$OT = \frac{1}{3}np + \frac{2}{3}nq = \frac{3}{4}p + nq - \frac{3}{4}mp$$

B1

M1

A1

B1

$$\begin{aligned}
 \frac{1}{3n} &= \frac{3}{4} - \frac{3}{4m} \dots \dots \dots i \\
 \frac{2}{3}n &= m \dots \dots \dots ii \\
 \frac{1}{3n} &= \frac{3}{4} - \frac{3}{4} \frac{2}{3}n \\
 \frac{1}{3}n &= \frac{3}{4} - \frac{1}{2}n \\
 \frac{1}{3n} + \frac{1}{2} &= \frac{3}{4} \\
 \frac{5}{6}n &= \frac{3}{4} \\
 n &= \frac{3}{4} \times \frac{6}{5} \\
 n &= \frac{9}{10} \\
 m &= \frac{2}{3} \times \frac{9}{10} \\
 m &= \frac{3}{5} \\
 ST &= \frac{3}{5}SQ
 \end{aligned}$$

$$TQ = \frac{2}{5}SQ$$

T is common

M1

M1

A1

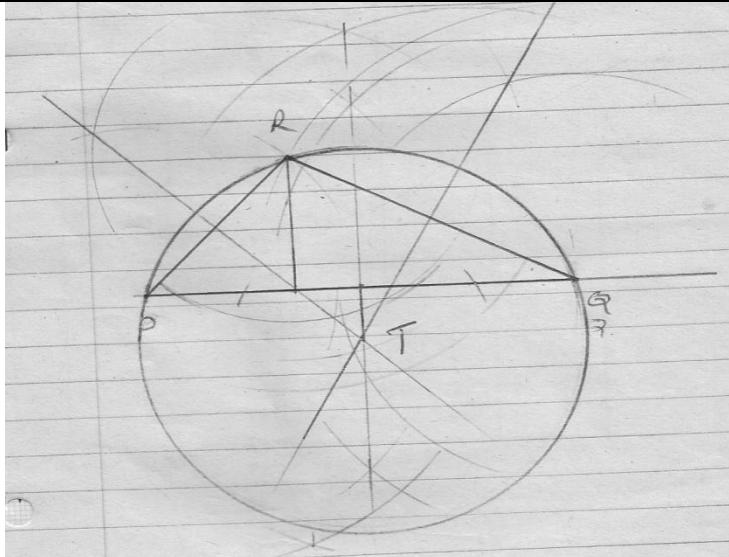
B1

B1

B1

10

22



$$\begin{aligned}
 TR &= 4.2 \text{ km} \\
 c \text{ shortest distance} & 1.2 \text{ km} \\
 d \text{ height} & 2.9 \\
 \frac{1}{2} \times 8 \times 2.9 &
 \end{aligned}$$

=11.6 km²

B1

B1

B1

B1

B1

B1

M1

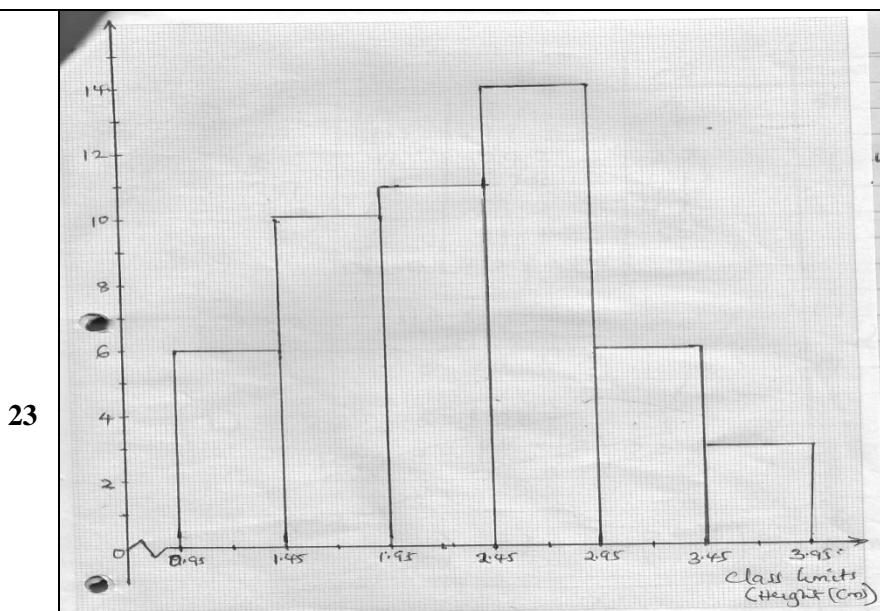
A1

*location of P
location Q
location R*

at least 2 bisector

T located

perpepndicular drawn value



(a)

x	f	xf	cf
1.2	6	7.2	6
1.7	10	17	16
2.2	11	24.2	27
2.7	14	37.8	41
3.2	6	19.2	47
3.7	3	11.1	50
	$\Sigma f=50$	$\Sigma Xf=116.5$	

$$mean \frac{116.5}{50} \\ = 2.33$$

b) 25th and 26th

$$1.95 + \frac{25 - 16}{11} 0.5 + 1.95 + \frac{26 - 16}{11} 0.5 \\ 2$$

$$\frac{1.95 + 0.4091}{2.35 + 2.4045} \\ 2 \\ 2.382$$

(c)

B1 \checkmark and pnts

B1 \checkmark xf

M1

A1

B1 \checkmark cf

M1

A1

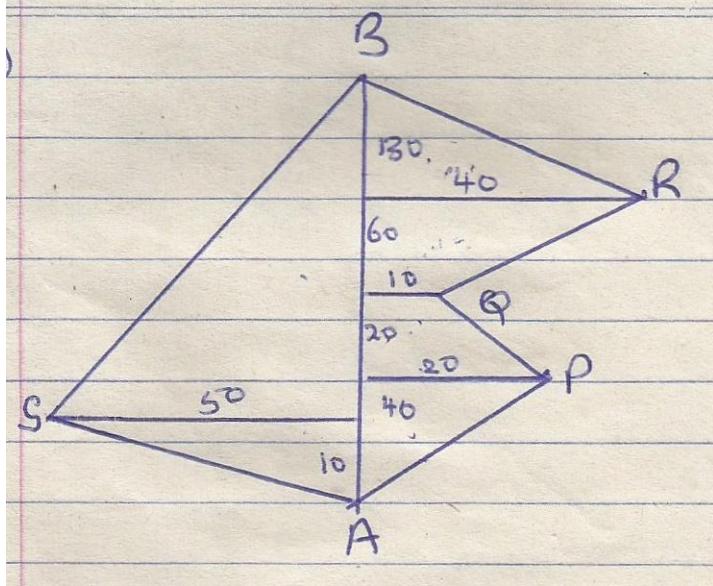
B2 all \checkmark bars
10 b1 4 \checkmark bars

24. (a)

B2 \checkmark right side for 2 \checkmark

B1 \checkmark left side

B1 \checkmark measurement



B1

Pts labeled

B2

Atleast labeled

M1

A1

10

$$\frac{1}{2} \times 10 \times 50$$

$$\frac{1}{2} \times 50 \times 250$$

$$\frac{1}{2} \times 20 \times 50$$

$$\frac{1}{2} (10+20)20$$

$$\frac{1}{2} (40+10)60$$

$$\frac{1}{2} \times 40 \times 130$$

$$\frac{1}{2} (500+1250+1000+600+3000+5200)$$

$$\frac{1}{2} \times x \times 11550$$

$$\frac{5775}{1000}$$

$$0.5775 \text{ ha m}$$