

MATHS PAPER 1 MARKING SCHEME

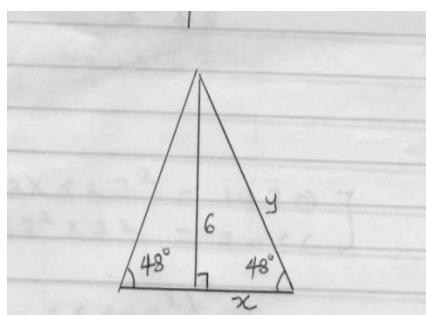
EMBU NORTH SUB COUNTY 2018

1	$\sqrt{\frac{0.38 \times 0.23 \times 2.7 \times 10^7}{0.114 \times 0.0575 \times 10^7}}$ $= \frac{38 \times 23 \times 27 \times 100}{114 \times 575}$ $\sqrt{36}$ $= \pm 6$	M1  M1  A1
2	$\frac{4(2x - 3) - 6(x - 2) - 3(1 - x)}{12}$ $\frac{8x - 12 - 6x + 12 - 3 + 3x}{12}$ $\frac{5x - 3}{12}$	M1  M1  A1
3	$2.456 \times 10^1$ $0.4072 \times 10^{-1} = 0.04072$ $4.362^2 = 19.027$ $0.04072 + 19.027$ $= 19.06772$ <p>19.07 correct to 4 s.f</p>	M1  M1  A1
4	$5000 \times 84.15 = \text{Ksh } 420750$ $\text{Ksh } \underline{289000}$ $\text{Ksh } 131750$ $\underline{131750}$ $121.47$ $= 1084.63$	M1  M1  A1

5	<p>External vol= <math>240 \times 30 \times 20</math>  <math>= 144000\text{cm}^3</math></p> <p>Internal volume = <math>237 \times 27 \times 17</math>  <math>= 108783 \text{ cm}^3</math></p> <p>volume of wood = <math>144000 - 108783</math>  <math>= 35217</math></p> <p>Mass = <math>35217 \times 0.4</math>  <math>= 14086.8\text{g}</math>  <math>= 14.0868 \text{ kg}</math></p>	M1 M1 M1 A1
6	$X + \frac{1}{3}x = 180^\circ$ $\frac{4}{3}x = 180^\circ$ $\frac{4}{3} \times \left(\frac{3}{4}\right) = 180^\circ \left(\frac{3}{4}\right)$ $X = 135^\circ$ External Angle = $180^\circ - 135^\circ = 45^\circ$ $\frac{360^\circ}{45^\circ} = 8 \text{ sides}$	M1 A1
7	$2x^2 + xy - y^2 = (2x - y)(x + y)$ $x^2 - y^2 = (x + y)(x - y)$ $\frac{(2x - y)(x + y)}{(x + y)(x - y)} = \frac{2x - y}{x - y}$	M1 M1 A1
8	$Y \leq 3$ $Y = -X + 3$ $Y \geq -X + 3$ $Y > X$	B1 B1 B1
9	<p>Centre <math>\left(\frac{-2+4}{2}, \frac{6+-2}{2}\right)</math></p> <p>(1,2)</p> <p><math>M1 = \frac{-2-6}{4-2} = \frac{-8}{6} = \frac{-4}{3}</math></p> <p><math>M2 = \frac{3}{4}</math></p> <p><math>\frac{Y-2}{X-1} = \frac{3}{4}</math></p> <p><math>4Y - 8 = 3X - 3</math></p> <p><math>4Y = 3X + 5</math></p> <p><math>Y = \frac{3X}{4} + \frac{5}{4}</math></p>	B1 M1 A1

10		<PQR B1 <PQR B1 L B1
11	<p>3 years ago son x  Now son <math>x + 3</math>  Father <math>3x + 3</math>  In 3 years time  Son <math>x + 3 + 3</math>  Father <math>3x + 3 + 3</math>  <math>X + 6 + 3x + 6 = 76</math>  <math>4x + 12 = 76</math>  <math>4x = 64</math>  <math>X = 16</math>  Present ages  Son = <math>16 + 3 = 19</math> years  Fathers = <math>3 \times 16 + 3 = 51</math> years</p>	B1 M1 A1
12	$2^{3x} = 2^{4y+2}$ $2 = 2$ $3x - 4y = 2 \dots \text{(i)}$ $36x = 3^{2y-6}$ $6x - 2y = -6 \dots \text{(ii)}$ $\begin{array}{rcl} 6x - 8y &=& 4 \\ 6x - 2y &=& -6 \\ \hline -6y &=& 10 \end{array}$ $y = \frac{-5}{3}$ $X = \frac{-14}{9}$	M1 M1 attempting to solve A1 for both answers

13



$$\tan 48^\circ = \frac{6}{x} = 5.4$$

$$\sin 48^\circ = \frac{6}{y} = 8.07$$

$$5.4 \times 2 = 10.8 + 8.07 + 8.07$$

$$= 26.940$$

$$= 26.94 \text{ cm}$$

M1

M1

A1

14

$$(5 \times 3) 3 + (\frac{1}{2} \times 3^2 \sin 60^\circ) 2$$

$$45 + 3.8971$$

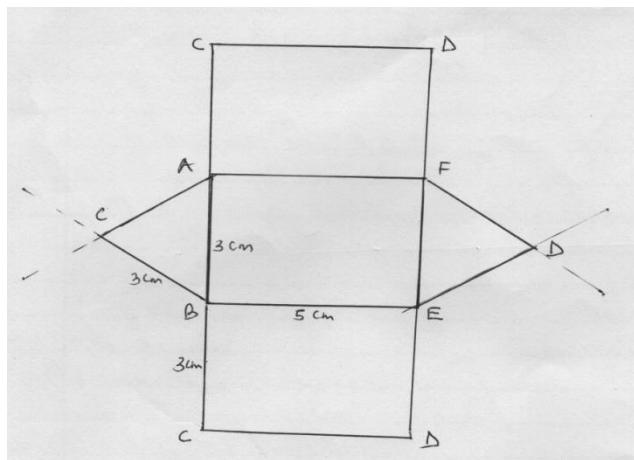
$$52.7942 \text{ cm}^2$$

M1

A1

B1 for correct measurement

B1 Labelled



15

$$P = 5 \binom{3}{2} - 2 \binom{4}{1} \\ = \binom{15}{10} - \binom{8}{2}$$

$$= \binom{7}{8}$$

$$P = \sqrt{7^2 + 8^2}$$

B1

M1

	= 10.63	A1																												
16	$2 \times 3 \times 5 \times 7^2 = 1470$ $2^4 \times 3^2 \times 7^2 = 7056$ $(2 \times 3 \times 5 \times 7^2)$ $\sqrt{(2^4 \times 3^2 \times 7^2)}$ $\frac{2^2 \times 3^2 \times 5^2}{2^2 \times 3 \times 7}$ $3 \times 5^2 \times 7^3$	M1 M1 A1																												
17a	70																													
b	<table border="1"> <thead> <tr> <th>Age ( years )</th> <th>x</th> <th>F</th> <th>xf</th> </tr> </thead> <tbody> <tr> <td>0 – 5</td> <td>2.5</td> <td>14</td> <td>35</td> </tr> <tr> <td>5-15</td> <td>10</td> <td>41</td> <td>410</td> </tr> <tr> <td>15 – 25</td> <td>20</td> <td>59</td> <td>1180</td> </tr> <tr> <td>25 – 45</td> <td>35</td> <td>70</td> <td>2450</td> </tr> <tr> <td>45 – 75</td> <td>60</td> <td>15</td> <td>900</td> </tr> <tr> <td></td> <td></td> <td><math>\Sigma f = 199</math></td> <td></td> </tr> </tbody> </table>	Age ( years )	x	F	xf	0 – 5	2.5	14	35	5-15	10	41	410	15 – 25	20	59	1180	25 – 45	35	70	2450	45 – 75	60	15	900			$\Sigma f = 199$		B1 B1
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c	<p>Mean <math>x = \frac{4975}{199} = 25</math> years</p> <p>On the graph paper</p>	A1																												
18 a i)	<p>kisumu —————— Nairobi</p> <p>9.30a.m</p> <p>Bus 81km/hr</p> <p>Distance covered by bus by 10.10</p> $81 \times \frac{40}{60} = 54\text{km}$ <p>Time taken for the two to meet</p>	M1 M1																												

	$\frac{360 - 54}{(81 + 72)}$ 2 hrs	A1
ii	$72 \times \frac{40}{60} = 48\text{km}$ Dist. By bus 40min= 54km + 48km = 102km apart	M1 A1
b. i	Dist. covered by the bus at 9.50a.m $81 \times \frac{20}{60} = 27\text{km}$ Time taken for the car to catch up $\frac{27}{90-81} = \frac{27}{9} = 3\text{hrs}$ $9.50\text{a.m} + 3.00 = 12.50\text{p.m}$	M1 M1 A1
ii	$81 \times 3 \frac{20}{60}$ = 270km $360 - 270$ 90km	M1 A1
19a	$\frac{8}{3} = \frac{4+x}{x}$ $8x = 12 + 3x$ $5x = 12$ $x = 2.4\text{cm}$ $2.4+4=6.4\text{cm}$	B1 M1 A1
b.	$V = \left(\frac{1}{3} \times \frac{22}{7} \times 8^2 \times 6.4\right) - \left(\frac{1}{3} \times \frac{22}{7} \times 3^2 \times 2.4\right)$ 429.105 – 22.629 406.48m <sup>3</sup>	M2 M1 A1
c.	$V = \frac{2}{3} \times \frac{22}{7} \times 27$ = 56.57cm Total volume = 406.48 + 56.57	M1 M1

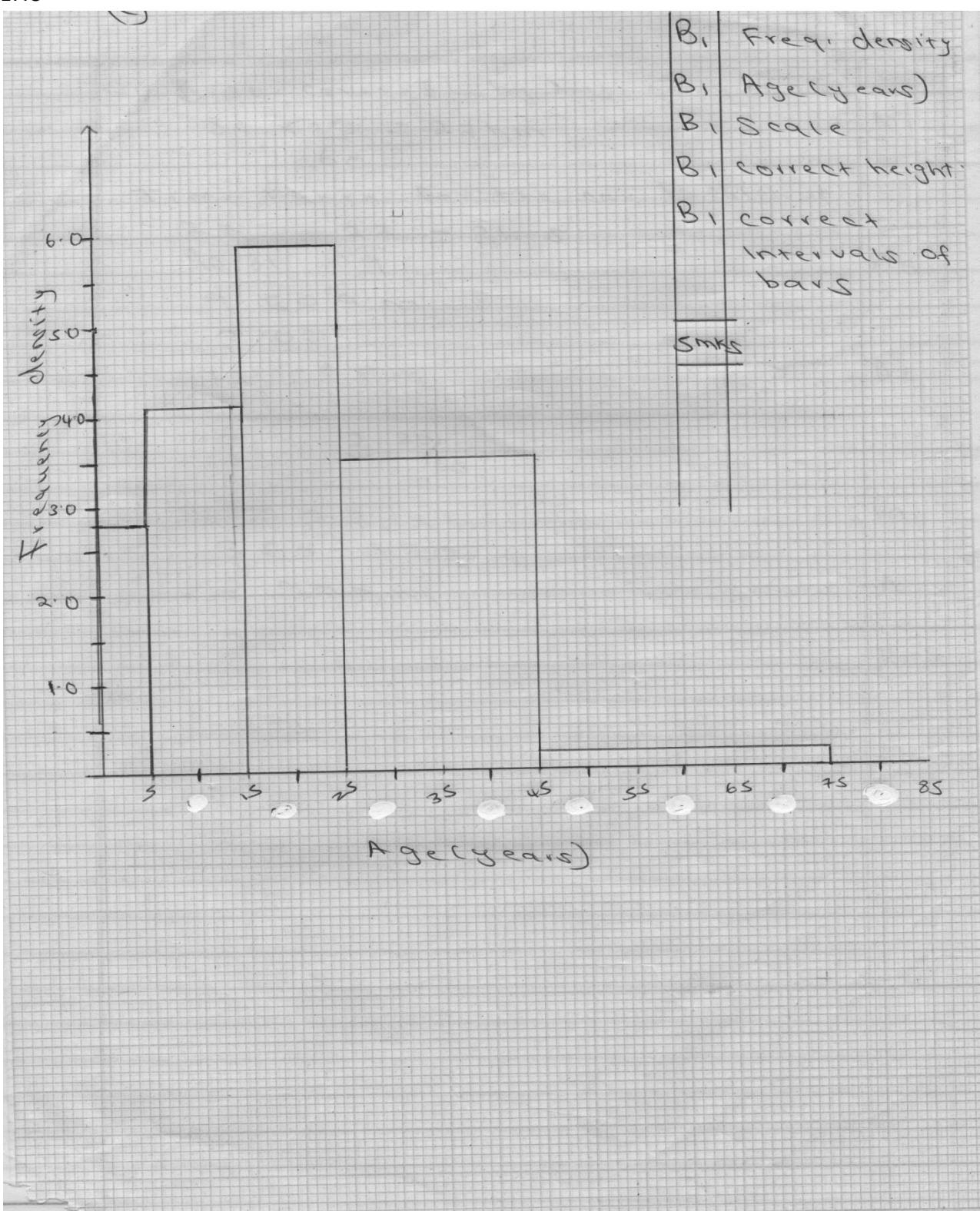
	= 463.05cm <sup>3</sup>	A1												
20. a	<p>Q 20.</p> <p> <math>S_1</math> Scale appropriately, used  <math>B_1</math> Location of point A  <math>B_1</math> Location of point C  <math>B_1</math> Location of ship S.     </p>													
b														
i	$AS = (10.1 \pm 0.1) \times 20 = 202 \pm 2\text{km}$	B1												
ii	Bearing of S from C = $276^\circ \pm 1^\circ$	B1												
iii	$B \text{ to } C = (13 \pm 0.1) \times 20 = 260 \pm 2\text{km}$	B1												
iv	Perpendicular distance of C from A = $(8.5 \pm 0.1) \times 20 = 170 \pm 2\text{km}$	B1												
v.	Compass Bearing of S from A = S $45^\circ W$	B1												
21.a	<table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 33.33%;"></th> <th style="width: 33.33%; text-align: center;">Tonnes</th> <th style="width: 33.33%; text-align: center;">dist</th> <th style="width: 33.33%; text-align: center;">cost</th> </tr> </thead> <tbody> <tr> <td></td> <td style="text-align: center;">48</td> <td style="text-align: center;">28</td> <td style="text-align: center;">sh.24000</td> </tr> <tr> <td></td> <td style="text-align: center;">96</td> <td style="text-align: center;">49</td> <td style="text-align: center;">x</td> </tr> </tbody> </table> $X = \frac{96}{48} \times \frac{49}{28} \times 24000$ $= \text{sh.}84000$		Tonnes	dist	cost		48	28	sh.24000		96	49	x	$B_1 \text{ for } \frac{49}{28}$ $B_1 \text{ for } \frac{96}{48}$ $M_1 \text{ mult}$ $A_1 \text{ (CAO)}$
	Tonnes	dist	cost											
	48	28	sh.24000											
	96	49	x											
b.	Expenditure $\frac{96}{8} \times 3000$ $= \text{sh } 36000$  Total = $84000 - 36000$	M1 A1												

	Profit sh 48000	B1									
c	$144 - 96 = 48 \text{ tonnes}$ <table style="margin-left: 40px;"> <tr><td>Tonnes</td><td>dist</td><td>amount</td></tr> <tr><td>48</td><td>28</td><td>24000</td></tr> <tr><td>48</td><td>84</td><td>y</td></tr> </table> $Y = \frac{84}{28} \times 24000$ $= \text{sh.} 72000$ $\text{Transport cost } \frac{100}{144} \times 72000$ $\text{Sh } 50,000$	Tonnes	dist	amount	48	28	24000	48	84	y	M1     M1     A1
Tonnes	dist	amount									
48	28	24000									
48	84	y									
22a.i	$\begin{array}{r} 12000 \\ \times \\ \hline \end{array}$     ii $\begin{array}{r} 14000 \\ \times -5 \\ \hline \end{array}$     $\frac{12000}{x-5} + 100$	B1     B1     B1									
b	$\frac{14000}{x-5} - \frac{12000}{x} = 100$     $14000x - 12000x - 60000 = 100x(x-5)$ $X^2 - 25x - 600 = 0$     $X = \frac{25 \pm \sqrt{625+2400}}{2}$ $\frac{25 \pm 55}{2}$ $X = 40$	M1     M1     M1     A1									
c	$\frac{14000}{35} = 400 \quad \frac{1200}{40} = 3000$     300: 400	M1     B1     A1									

	3:4	
23	Graph paper	
24a	$S = 2(5^3) + 4(5)^2 - 8(5) + 3$ $= 250 + 100 - 40 + 3$ $= 313\text{m}$	B1 A1
b.	$6t^2 + 8t - 8$ $t=5$ $6(5^2) + 8(5) - 8$ $150 + 40 - 8$ $182\text{m/s}$	B1 M1 A1 B1
c.	$V = 0$ $6t^2 + 8t - 8 = 0$ $2(3t - 2)(t + 2) = 0$ $t = \frac{2}{3} \text{ or } t = -2$ $t = \frac{2}{3}$	M1 A1 B1
d	$6t^2 + 8t - 8$ $12t + 8$ $t = 2$ $12(2) + 8$ $32\text{m/s}^2$	A1



17.C



Q23.

