

121/1
MATHEMATICS
JULY, 2018
PAPER 1
TIME: 2½ HOURS

BUURI EAST STANDARDS

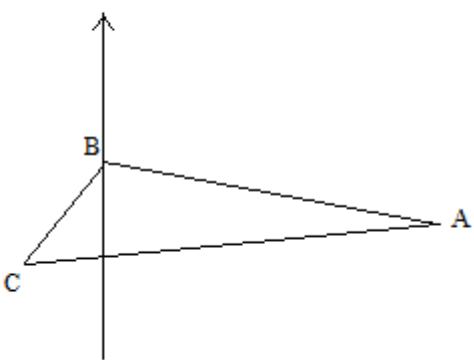
Kenya Certificate of Secondary Education
MATHEMATICS Alt. A

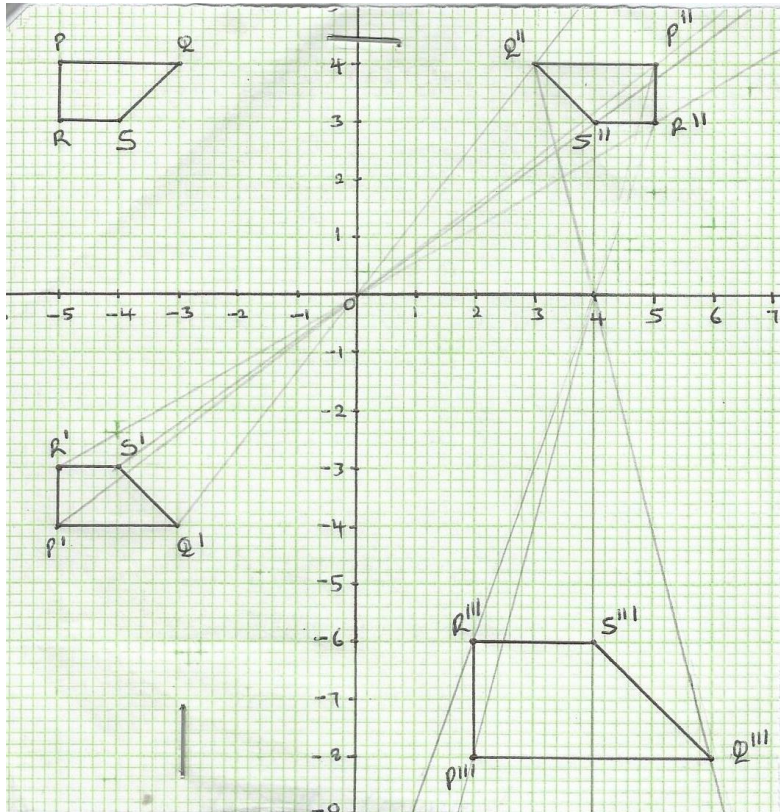
MARKING SCHEME

No.	Calculations	Marks	Remarks
1.	Numerator $-18 + 2$ -14 <u>Denominator</u> $18 + -11$ 7 $\frac{-14}{7}$ -2	B1 B1 B1	For -14 For 7 For -2 evidence of the operation must be seen
		3	
2.	Fraction walked = $1 - \frac{1}{4}$ $= \frac{3}{4}$ Actual distance walked = $\frac{3}{4} \times \frac{32}{5}$ $= \frac{24}{5}$ $= 4 \frac{4}{5} \text{ km}$	M1 M1 A1	
		3	
3.	1st commission $\frac{2}{100} \times 200\,000$ 4 000 2nd commission $\frac{4}{100} \times (600\,000 - 200\,000)$ 16 000 Total 20 000 + 4 000 <u>16 000</u> Sh. 40 000	M1 M1 A1	Process of getting the two commissions For process of getting total pay CAO
		3	

4		B1 B1 B1	All lines 01 ✓ 1y drawn to be actual length. No use of scale All angles 01 ✓ 1y drawn ✓ shape of net
5	$2^{3y+3} - 2^{3y+1} = 48$ $2^{3y} (2^3 - 2) = 48$ $2^{3y} = 48/6$ $2^{3y} = 8$ $2^{3y} = 2^3$ $y = 1$	3 M1 M1 A1	Index form Equating 2^{3y} to 8 accept equivalent
6	Numerator $12x^2 - 8ax + 9ax - 6a^2$ Denominator $(3x + 2a)(3x - 2a)$ $\frac{(3x - 2a)(4x + 3a)}{(3x + 2a)(3x - 2a)}$ $\frac{4x + 3a}{3x + 2a}$	M1 M1 A1	Factorising num ✓ 1y Factorizing den correctly Must be extracted
		3	
7	Gradient of Q = $1/3$ $\frac{Y - 6}{X - 3} = \frac{1}{3}$ $3y = x + 15$ $Y = \frac{1}{3}x + 5$	B1 M1 A1	Must be in the form $Y = mx + c$
		3	

8.	$\frac{1}{1 - \frac{1}{\sqrt{2}}} = \frac{1}{\sqrt{2} - 1}$ $= \frac{\sqrt{2}(\sqrt{2}+1)}{(\sqrt{2}-1)(\sqrt{2}+1)}$ $= \frac{2+\sqrt{2}}{2-1}$ $= 2 + \sqrt{2}$	M1 M1 A1	Replacing π 45 with 2 Rationalizing CAO
		3	
9	$b^2 = 6^2 + 11^2 - 2 \times 6 \times 11 \times \cos 100^\circ$ $b^2 = 179.92$ $b = 179.92$ $= 13.41$	M1 M1 A1	Substituting in cosine rule
		3	
10.	$V = \frac{1}{2} \times 4 \times 6 \times 20$ $= 240$ $M = 240 \times 1.25$ $= 300$	M1 M1 A1	
		3	
11	$\text{Total time taken} = 90 + 15 + 5$ $= 110 \text{ minutes}$ $= 1 \text{ hr } 50 \text{ minutes}$ $1500 \text{ h} + 1 \text{ h } 50 \text{ min}$ 1650 h	M1 M1 A1	
		3	
12	$X \geq -4$ $Y + x \leq 0$ $Y - \frac{3}{4}x > -6$	B1 B1 B1	
		3	
13	$L(1 - 16) = 132$ $L^2 - 16L - 132 = 0$ $(L - 22)(L + 6) = 0$ $L^2 = 22 \text{ or } L = -6 \text{ (Impossible)}$ $L = 22$ $P = 2(22 + 6) = 56$	M1 M1 A1 B1	Attempt to get equation Attempt to solve for L Evidence of discrimination seen

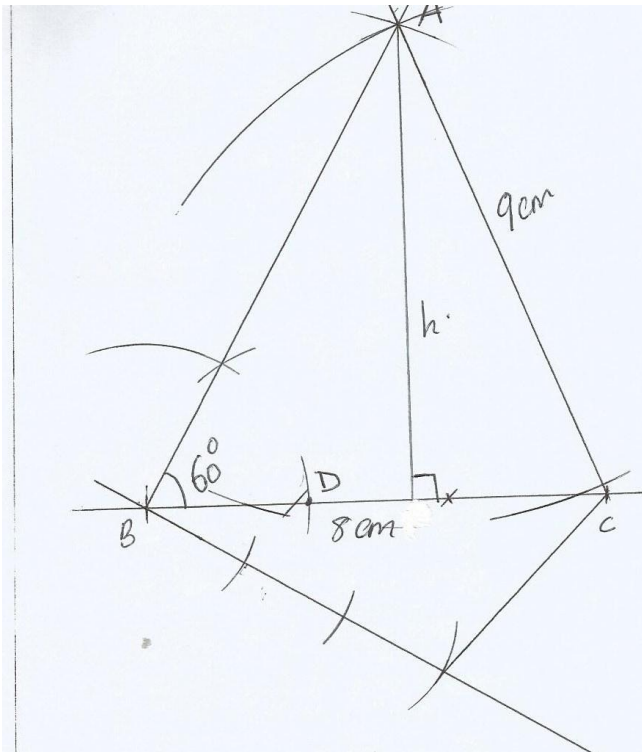
		4	
14	 CB = 1.2 x 20 = 24km	B1 B1 B1 B1	Locating C ✓ly Form 24km
15	a) $\frac{1}{2} \begin{matrix} 2 & -4 \\ -3 & 7 \end{matrix} = \frac{1}{-3/2} \begin{matrix} 1 & -1 \\ 7/2 & 7/2 \end{matrix}$ b) $\begin{matrix} 1 & -1 & 7 & 4 \\ -3/2 & 7/2 & 3 & 2 \end{matrix} \begin{matrix} x \\ y \end{matrix} = \begin{matrix} 1 & -1 \\ -3/2 & 7/2 \end{matrix} \begin{matrix} 14 \\ 8 \end{matrix}$ X = 6 Y = 7 X = 6 Y = 7	4 B1 M1 A1	 Premultiplying Both values of x and y. must be extracted
16	0.6511 x 1/10 + 3 (0.7656) 0.06511 + 2.3058 2.37091 1.5398	3 M1 M1 A1	
		3	

17.	 c) i) P'Q'R'S' and P''Q''R''S'' are directly cogent ii) Oppositely congruent PQRS and P'Q'R'S' PQRS and P''Q''R''S''	B1 B1B1 B2 B2 B1 B1 B1	VPQRS P'Q'R'S Located P''Q''R''S ✓ located P'''Q'''R'''S''' ✓ located
		10	
18	a) $\frac{x}{x+12} = \frac{5}{10}$ $10x = 5x + 60$ $5x = 60$ $x = 12$ $L = 24^2 + 102 = 26$ $1/26 = 5/10$ $L = 13$ Slant height $26 - 13$ $= 13$	M1 M1 A1	When 13 is seen

	b) Curved area of the frustum $S.A = \pi RL - \pi rl$ $= \pi (260 - 65)$ $= 612.6$ c) Volume of the frustum $\frac{1}{3} \pi (R^2H - r^{2h})$ $= \frac{1}{3} \pi (2400 - 300)$ $= \frac{1}{3} \pi (2100)$ $= 2200 \text{ cm}^2$	M1 M1 A1 M1M1M1 A1	Both reas correct ✓ -
	Total marks	10	
19	i) $1 \frac{1}{2} \times 80$ $= 120\text{km}$ ii) $120 - 50$ $= 40$ iii) Time taken $\frac{120}{40}$ $= 3\text{hrs}$ $8.300 + 3$ 11.30cm iv) 3×120 $= 360\text{km}$ v) $600 - 360 = 240\text{km}$	M1 A1 M1 A1 M1 A1 B1 M1 A1 B1	For 11.30am For 240
	Total marks	10	

20	<table><tr><th>Class</th><th>Tally</th><th>Frequency</th><th>Mid point</th><th>Fx</th><th>Cf</th></tr><tr><td>145 – 149</td><td>11</td><td>2</td><td>147</td><td>294</td><td>2</td></tr><tr><td>150 – 154</td><td>1</td><td>1</td><td>152</td><td>152</td><td>3</td></tr><tr><td>155 – 159</td><td>1</td><td>11</td><td>157</td><td>1727</td><td>14</td></tr><tr><td>160 – 164</td><td></td><td>5</td><td>162</td><td>810</td><td>19</td></tr><tr><td>165 – 169</td><td>11</td><td>7</td><td>167</td><td>1169</td><td>26</td></tr><tr><td>170 – 174</td><td>11</td><td>7</td><td>172</td><td>1204</td><td>33</td></tr><tr><td>175 - 179</td><td>111</td><td>3</td><td>177</td><td>531</td><td>36</td></tr><tr><td></td><td></td><td></td><td></td><td>Fx^2 5887</td><td></td></tr></table> b) i) $\frac{5887}{36}$ $= 163.53$ ii) $159.5 \frac{(36 - 14) \times 5}{11}$ $= 159.5 + 1.8182$ $= 161.32$ d) Graph	Class	Tally	Frequency	Mid point	Fx	Cf	145 – 149	11	2	147	294	2	150 – 154	1	1	152	152	3	155 – 159	1	11	157	1727	14	160 – 164		5	162	810	19	165 – 169	11	7	167	1169	26	170 – 174	11	7	172	1204	33	175 - 179	111	3	177	531	36					Fx^2 5887		B1 B1 B1 B1 A1 M1 A1 B1 B1	✓ classes ✓ frequencies (all rallies) ✓ ΣFx (frequency) Σ midpoints ✓ Cumulative Frequency (c.f) ✓ Plotting ✓ curve (No hanging curve. Not drawn by use of free hand)
Class	Tally	Frequency	Mid point	Fx	Cf																																																				
145 – 149	11	2	147	294	2																																																				
150 – 154	1	1	152	152	3																																																				
155 – 159	1	11	157	1727	14																																																				
160 – 164		5	162	810	19																																																				
165 – 169	11	7	167	1169	26																																																				
170 – 174	11	7	172	1204	33																																																				
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	Total marks	10																																																							

21	a) i) $\frac{16200}{Y}$ ii) $\frac{16\ 200}{y+3}$ or $\frac{16\ 200}{y} - 60$ b) i) $\frac{16\ 200}{y} - \frac{16\ 200}{y+3} = 60$ $60y^2 + 180y - 48\ 600 = 0$ $Y^2 + 3y - 810 = 0$ $Y = -3 + 570 (y + 30) (y - 27) = 0$ $= 27 \text{ or } -30$ $= y = 27$ ii) $\frac{16200}{30} = \text{Ksh } 540$ iii) $\frac{15}{100} \times \frac{16\ 200}{27}$ $= \text{Ksh } 90$	B1 B1 M1 M1 M1 A1 M1A1 M1 A1	Simplifying and removing brackets Factors equated to zero Evidence of discrimination of -30 seen
Total marks		10	

22		B1 B1 B1 B1 600 ✓ constructed locating point A Dropping a Length the 8.2 ± 0.1 B1 B1 B1 For a line at an angle to BC For joining C to the last point For locating point D M1A1 (following through)	
Total marks		10	

23	a) i) $BN = BA + AN$ $= -a + \frac{5}{6}b$ $= \frac{5}{6}b - a$ ii) $CM = -b + r \text{ cm}$ $= b + r \left(\frac{2}{5}a - b \right)$ i) $AX = b + r \text{ cm}$ $= b - rb + \frac{2}{3}ra$ $= (1 - r)b + \frac{2}{5}ar$ $Ax = a + K \left(\frac{5}{6}b - a \right)$ $A - ka + \frac{5}{6}kb$ ii) $(1 - r)b + \frac{2}{5}ar = (1 + k)a + \frac{5}{6}kb$ $\frac{5}{6}K = 1 - r - (i)$ $\frac{2}{5}r = 1 - k \quad \text{-- (11)}$ $K = \frac{6}{5} - \frac{6}{5}r$ $\frac{2}{5} = 1 - \left(\frac{6}{5} - \frac{6}{5}r \right) = 1 - \frac{6}{5} + \frac{6}{5}r$ $-4r = -1 \Rightarrow r = \frac{1}{4}$ $\frac{5}{6}K = \frac{3}{4}$ $K = \frac{9}{10}$	B1 B1 M1 M1 M1 M1 Al	Equating two values of AX. Two equations extracted
		10marks	
24a)	$S = t(t^2 - t - 2t + 2)$ $= t^3 - 3t^2 + 2t$ $\frac{ds}{dt} = 3t^2 - 6(2) + 2$ $V = 3(4) - 6(2) + 2$ $V = 2 \text{ m/s}$ b) $\frac{dv}{dt} = 0$ $\frac{dv}{dt} = 6t - 6$		B1 M A1 M1

c)	$6t - 6 = 0$		
	$t = 1$		M1
	$= 3(1)^2 - 6(1) + 2$		A1
	$= -1\text{m/s}$		
d)	$3t^2 - 6t + 2 = 0$		M1
	$T = 6 + \frac{(-6)^2 - 4(3)(2)}{2(3)}$		
	$T = 6 + 3.464$		A1
	$T = 1.577 \text{ or } 0.4227$		
	$a = 6(3) - 6 = 12\text{m/s}^2$		B1
	Total marks	10	

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