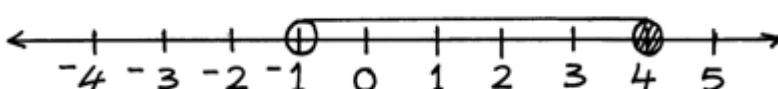

KENYA NATIONAL EXAMINATION COUNCIL
REVISION MOCK EXAMS 2016
TOP NATIONAL SCHOOLS

PRECIOUS BLOOD HIGH SCHOOL
MATHEMATICS
PAPER 1

PRECIOUS BLOOD KCSE TRIAL AND PRACTICE EXAM 2016

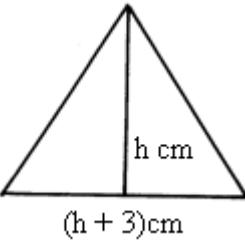
PAPER 1

MARKING SCHEME

1	$\sqrt{\frac{38X23X27X100}{114X575}}$ $\sqrt{\frac{38X23X27X100}{114X575}} \quad \sqrt{36} \quad = \pm 6$	M ₁ M ₁ A ₁	Removing the decimals Division Correct square root
		03	
2	$y = a + b(x - c)$ $y = 4 + 6(3 - 2)$ $y = 4 + 5$ $= 11x25$ $= 275$	M ₁ M ₁ A ₁	Correct substitution
		03	
3	$3 - 2x < 5$ $-2x < 2$ $x > -1 \quad \dots \dots \dots \text{(i)}$ $4 - 3x \geq -8$ $-3x \geq -12$ $x \leq 4 \quad \dots \dots \dots \text{(ii)}$ $-1 < x \leq 4$ 	B ₁ B ₁ A ₁	Check on inequality symbols Correct illustration
		03	
4	$\sqrt{\frac{1}{2.456 \times 10^4}} + 4.346^2$ $\sqrt{10^{-1}} \cdot 4.072 + 18.88$ $\sqrt{18.92872}$ 4.3509	M ₁ M ₁	Correct reciprocal square

	4.351 ?(4 significant figure)	M1	Correct square root Correct significant figures
		A1	
		04	
5.	<p>Amount in ksh. $20,000 \times 147.56 = 2,951,200$</p> <p>Balance ksh. $2,951,200 - 2,510,200 = 441000$</p> <p>Into US dollars $\frac{441000}{74.50}$</p> <p>= 5919.46</p> <p>= 5919 US dollars.</p>	M1	
		M1	
		A1	
		03	
6.	<p>1,2,3,4,4,5,6,6,7,7,8,9</p> <p>$Q \Rightarrow \frac{1}{4} \times 12$</p> <p>= 3rd and 4th positions</p> <p>$Q_1 = 3.5$</p> <p>$Q_3 = 3.5$</p> <p>$Q_3 \Rightarrow \frac{3}{4} \times 12$</p> <p>9th and 10th positions $Q_3 = 7$</p> <p>$QD = \frac{1}{2} (Q_3 - Q_1) = \frac{1}{2} (7 - 3.5) = \frac{3.5}{2}$</p> <p>= 1.75</p>		
		03	

7.	$Q = \begin{pmatrix} 6 \\ 3 \end{pmatrix}; R = \begin{pmatrix} -4 \\ 2 \end{pmatrix}; U = \begin{pmatrix} 8 \\ -4 \end{pmatrix}$ $S \xrightarrow{Q} T$ \sim $T \xrightarrow{R} U$ \sim <p><i>Object + Translation vector = image vector</i></p> $T = \begin{pmatrix} 8 \\ -4 \end{pmatrix} - \begin{pmatrix} -4 \\ 2 \end{pmatrix} = \begin{pmatrix} 12 \\ -9 \end{pmatrix}$ $S = \begin{pmatrix} 12 \\ -6 \end{pmatrix} - \begin{pmatrix} 6 \\ 3 \end{pmatrix} = \begin{pmatrix} 6 \\ -9 \end{pmatrix}$ $co-ordinate\ of\ S = \langle 6, -9 \rangle$	M1	Column vector for T
		M1	Column vector for S
		A1	Co- ordinate
		03	
8.	<p>Mid point of CD</p> $\left(\frac{-7+3}{2}, \frac{8-8}{2} \right) = \langle 2, 0 \rangle$ <p>Gradient of C</p> $\frac{-3-8}{3+7} = \frac{-16}{10} = \frac{-8}{5} \Rightarrow G_1$ $G_1 G_2 = -1$ $\frac{-8}{5} G_2 = -1 \Rightarrow G_2 = \frac{5}{8}$ <p>Equation</p> $\frac{y}{x+2} = \frac{5}{8}$ $8y = 5x + 10$ $y = \frac{5}{8}x + \frac{5}{4}$	B1	Correct G_2
		M1	
		A1	Any of the two equatius
		04	
9.	M.P		

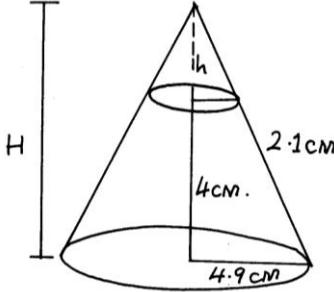
	$80\% = 160$ $100\% = \frac{100 \times 160}{80} = 200$ $Sp = 160\%$ $B.p = ?$ $130\% = 160$ $100\% = \frac{100 \times 160}{130} = Kshs 123.08$ $\% profit \left(\frac{200 - 123.08}{123.08} \right) 100$ 62.50%	M1 M1 A1	
		03	
10.	 $\frac{1}{2} \times (h + 3)h = 35$ $h^2 + 3h - 70 = 0$ $h^2 - 7h + 10h - 70 = 0$ $h(h - 7) + 10(h - 7) = 0$ $(h + 10)(h - 7) = 0$ $h = -10 \text{ or } 7$ $h = 7 \text{ cm}$	B1 A1	
		03	
11.	$2(x - 4) - 3(x - 1) = 6 - 5x$ $12x - 8 - 6x + 3 = 6 - 5x$ $11x = 11$ $x = 1$	M1 A1	
		02	
12.	$\frac{30}{360} \times \frac{22}{7} \times r^2 - \frac{1}{2} r^2 \sin 30^\circ = 5.25$ $\frac{1}{42} r^2 - \frac{1}{4} r^2 = 5.25$ $\frac{1}{84} r^2 = 441$ $r = \pm 21 \text{ cm}$ $r = 21 \text{ cm}$	M1 M1 A1	
		03	

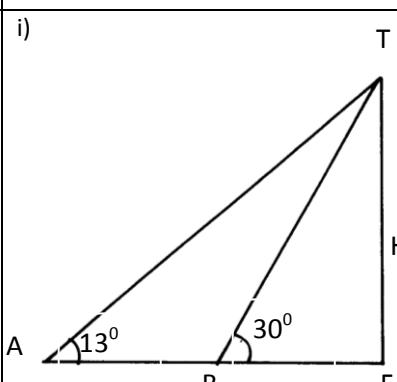
13.	<p>Let the number be xy</p> $10x + y = 5 \quad (1)$ $10x - y = 5x + 5y \quad (2)$ $5x - 4y = 0 \quad (3)$ $(1) + (2) \rightarrow 10x + x = 5x + 5y \rightarrow 9x = 5y \rightarrow 9$ $x - y = -1 \quad (4)$ <p>solving two equations simultaneously</p> $\begin{array}{r} x - y = -1 \\ 5x - 4y = 0 \\ \hline y = 5 \end{array}$ $x = -1 + 5 = 4$ $xy = 45$ <p>The number is 45</p>	M1	Equals
		A1	Solving equations
14.	<p>Area scale factor (Asf) = $\frac{12}{108} = \frac{1}{9}$</p> <p>Linear scale factor (L.s.f) = $\sqrt{\frac{1}{9}} = \frac{1}{3}$</p> <p>Volume scale factor (V.s.f) = $\left(\frac{1}{2}\right)^3 = \frac{1}{27}$</p> $27 = 810 \text{ cm}^3$ $1 = \left(\frac{310 \times 1}{27}\right) = 30 \text{ cm}^3$ <p>volume of smaller cone = 30 cm^3</p>	M1 M1 A1	Correct scale factors
15.	<p>Let the exterior angle be x</p> $x = 180 - x$ $x = \frac{1}{3}(180 - x)$ $3x = 180 - x$ $4x = 180$ $x = 45^\circ$ $\frac{360}{n} = 45$ $45n = 360$ $n = 8 \text{ sides}$ <p>The polygon is an octagon</p>	M1 M1 B1	
		03	

	$\frac{1}{3} \left\{ \frac{(80 - 2) \times 180}{n} \right\} = \frac{360}{n}$ $180n - 360 = 1080$ $n = 8$ <p>The polygon is octagon.</p>	M1 M1 B1	
		03	

16.	$\frac{1}{3} \Rightarrow food$ $\frac{1}{4} \Rightarrow rent$ $remainder = \left(\frac{1}{4} + \frac{1}{3} \right) = \frac{5}{12}$ $Transport = \frac{3}{5} \times \frac{5}{12} = \frac{1}{4}$ $Spent = \frac{1}{3} + \frac{1}{4} + \frac{1}{4} = \frac{5}{6} \Rightarrow 1800$ $He saved \frac{1}{6}$ $\frac{5}{6} = 1800$ $\frac{1}{6} = \frac{1}{6} \times 1800 \times \frac{6}{5}$ $= 360$	B1 M1 A1	
-----	---	----------------	--

17.a)	Cost price of the mixture $Ksh.(25 \times 5 + 30 \times 2 + 45 \times 1) = Ksh. 230$ Selling price $\left(\frac{120 \times 230}{100} \right) = ksh. 276$ Total kgs = $5 + 2 + 1 = 8$ Profit per kg of the mixture $\left(\frac{276 - 230}{8} \right)$ Ksh. 5.76 (i) the cost price after one year $\frac{112}{100} \times 230 = ksh. 257.60$ $profit \Rightarrow \frac{120}{100} \times 257.60 = 309.12$ $\frac{ksh. 309.12}{8} = 38.64$ Price per kg of the mixture = kshs. 38.64 ii) $40.25 - 32.2 = ksh. 8.05$	M1 M1 M1 A1 M1 M1 A1 M1 M1 M1 M1	For cost price For selling price Profit Price per kg
b)			

	$\% \text{ profit} = \frac{8.05}{32.2} \times 100$ 25%	A1	
		10	
18.a)	 $\frac{4+h}{h} = \frac{4.9}{2.1}$ $4.9h = 3.4 + 2.1h$ $2.8h = 3.4$ $h = 3\text{cm}$ $H = 3 + 4 = 7\text{cm}$	M1	
b)	<p>Surface area</p> $\text{Curved Surface Area} = \Pi r l + \Pi r^2 + 2\Pi R^2$ $L^2 = 4.9^2 + 7^2$ $= 24.01 + 49 = 73.01$ $L = 8.54\text{cm}$ $l^2 = 2.1^2 + 3^2 = 4.41 + 9 = 13.41$ $l = 3.66\text{cm}$	M1 M1 M1 A1	
	$3.142(4.9 \times 8.54) + 3.1 \times 3.66 + 2.1^2 + \times 4.9^2$ $3.142(1.846 - 7.686 + 4.41 + 48.02)$ $= 3.142 \times 86.59 \backslash 272.07\text{cm}^2$	M1 M1 M1 A1	
		10	
19.a)	<p>Area of the floor = $\frac{1960}{70} = 28\text{m}^2$</p> <p>Let the other length be y</p> $xy = 28\text{m}^2$ $y = \frac{28}{x}\text{m}$	M1 A1 B1	

b)	$\text{New area} = \left(1 - \frac{28}{x} - 1\right)m^2$ $\cos t = 70 \left(1 - \frac{28}{x} - 1\right)m^2$ $1960 - 70 \left(28 - x - \frac{28}{x} + 1\right) = 700$ $1960 - 1960 + 70x + \frac{1960}{x} - 70 = 700$ $70x^2 + 190 - 70x = 700x$ $70x^2 - 770x + 1960 = 0$ $x^2 - 11x + 28 = 0$	M1 M1 M1 B1	
c)	$x^2 - 11^2 + 28 = 0$ $x^2 - 7x - 4x + 28 = 0$ $x(x - 7)(x + 4) = 0$ $x = 7 \text{ or } 4$ <i>Dimensions are</i> <i>length = 7 cm when x is 7</i> <i>width = 4 cm when x is 7</i>	M1 B1	All correct
20.a)	i) 	A1	All correct
		10	

	$\frac{H}{x} = \tan 30^0$ $H = x \tan 30^0$ $\frac{H}{120+x} = \tan 13^0$ $H = (20+x) \tan 13^0$ <p>but $H = H$</p> $x \tan 30^0 = (20+x) \tan 13^0$ $0.5774x = 0.2309(20+x)$ $0.574x = 27.708 + 0.2309x$ $0.3465x = 27.708$ $x = 79.97M$ $H = 79.97 \tan 30^0$ $= 46.17M$	M1 M1 M1 A1																			
	ii) $\frac{46.17}{TB} = \sin 30^0$ $0.5TB = 46.17$ $TB = 92.3AM$	M1 A1																			
b)	$\tan 105^0 = \sin 30^0$ $\tan 15^0 = \frac{1}{2+\sqrt{3}}$ $\frac{2-\sqrt{3}}{4-3} = \frac{2-\sqrt{3}}{1}$ $2-\sqrt{3}$	M1 M1 A1																			
		03																			
21.a)	<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr> <tr> <td>y</td><td>7</td><td>-2</td><td>-7</td><td>-8</td><td>-5</td><td>2</td><td>13</td><td>28</td></tr> </table> <p>Correct scale</p> <p>Correct plotting</p> <p>Smooth curve</p>	x	-1	0	1	2	3	4	5	6	y	7	-2	-7	-8	-5	2	13	28	B1 B1 B1 B1 B1	Correct values
x	-1	0	1	2	3	4	5	6													
y	7	-2	-7	-8	-5	2	13	28													
b)	The roots of the function $2x^2 - 7x - 2 = 0$ are $x = -0.3 \pm 0.1$ $x = 3.8 \pm 0.1$	B1	All values correct																		

c)

$$Y = 2x - 7$$

P

x	0	2	3	4
y	-7	-3	-1	1

B1

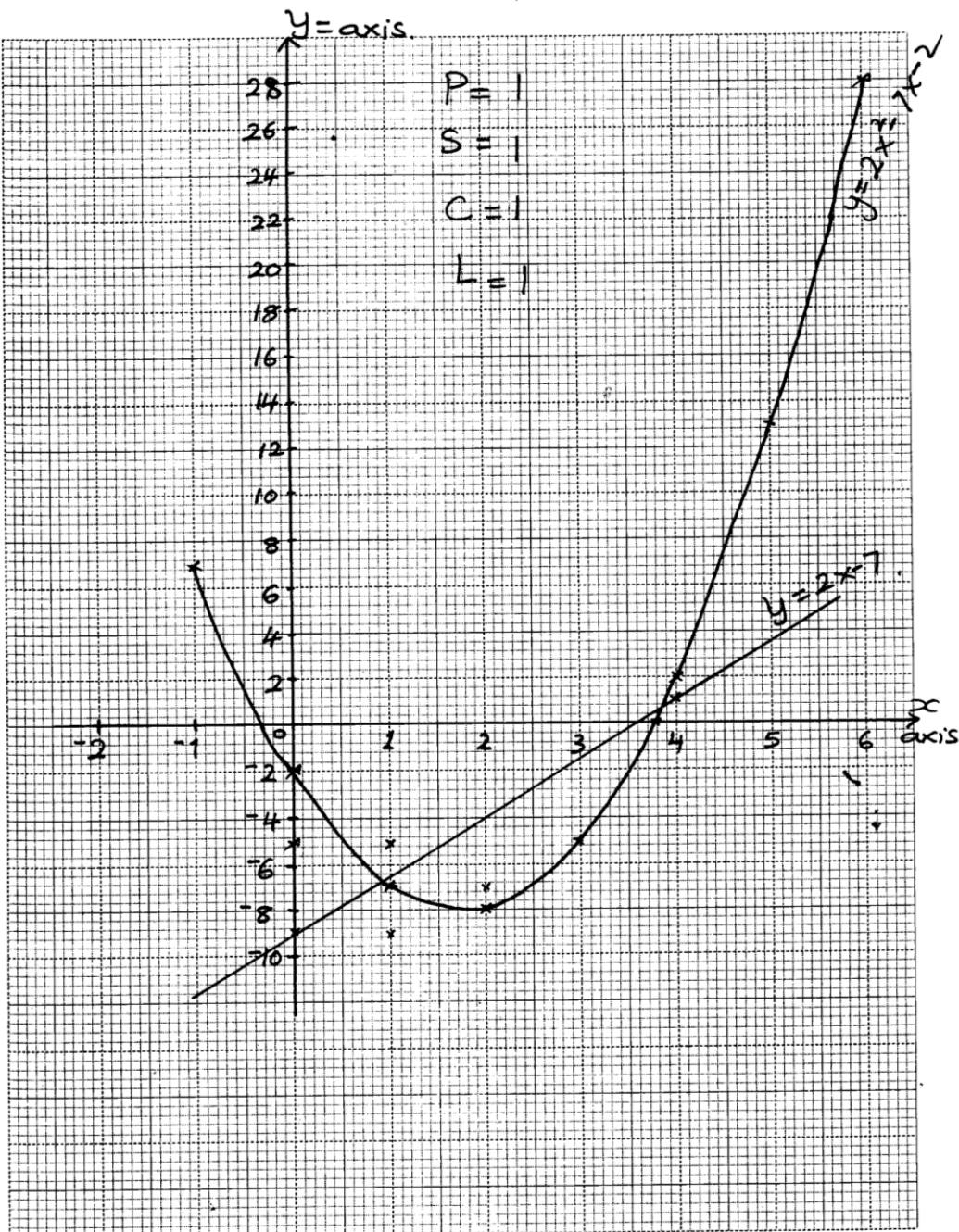
Table

B1 B1

Correct values of x

B1

Correct line graph.



Maths 121/1

M1 scheme

From the graph the values of x are

	$x = 0.65 \pm 0.05$ $x = 3.85 \pm 0.05$		
		10	
22.a)	<p>Person A alone</p> <p>All working takes $\frac{5}{3}$ hrs</p> <p>In 1 hr they do $\frac{3}{5}$ of the job</p> <p>Work done in 40 mins = $\frac{2}{3}$ hrs</p> <p>$\frac{2}{3} \times \frac{3}{5} = \frac{2}{5}$ of the job</p> <p>Assume A alone takes a hours, B alone b hrs and C alone $\frac{40}{9}$ hrs.</p> <p>When B left $\frac{2}{5}$ had been done</p> <p>\therefore A and C worked for $1/3$ hrs hence did</p> $\frac{1}{3} \left(\frac{1}{9} + \frac{9}{40} \right) = \frac{1}{39} + \frac{3}{40}$ <p>A alone did $\frac{1}{9} \left(\frac{53}{30} \right) = \frac{53}{309}$ hence</p> <p>Completing the job</p> $\frac{2}{5} + \frac{1}{39} + \frac{3}{40} + \frac{53}{309} = 1$ $\frac{63}{309} = \frac{21}{40}$ $= a = 4$		
b)	<p>Person B alone</p> $\frac{1}{4} + \frac{1}{b} + \frac{9}{40} = \frac{3}{5}$ $\frac{1}{b} = \frac{1}{8}$ <p>$\therefore b$ alone takes 8 hrs</p>		
c)	<p>Person A and C alone</p> $\frac{1}{4} + \frac{9}{40} = \frac{19}{40}$ in one hour $\therefore \text{take } \frac{40}{19} = 2 \frac{2}{19} \text{ hrs}$		
		10	
23.	<p>i) $\angle CDE = 180^\circ - \angle CBE = 180^\circ - 80^\circ = 100^\circ$ (Opposite angles of cyclic quadrilaterals)</p> <p>ii) $\angle EDF = 180^\circ - 100^\circ = 80^\circ$ ($\angle S$ of a straight line) $\angle DEF = 180^\circ - 110^\circ = 70^\circ$ ($\angle S$ on a straight line) $\angle DFE = 180^\circ - (30^\circ + 70^\circ) = 80^\circ$ (some of angles of a triangle)</p>	B1 B1	

	<p>iii) Obtuse angle COE $= 80 \times 2 = 160^\circ$ (angle subtended at the centre is twice angle subtended at the circumference by the same chord)</p> <p>iv) $\angle ADE = \angle ABE = 40^\circ$ $\angle S$ subtend by the same chord to the circumference.</p> <p>v) $\angle CAE = \frac{1}{2} \angle COE = \frac{1}{2} \times 160 = 80^\circ$ angle subtended at the centre is twice the one subtended by the same chord on the circumference.</p>	B1 B1 B1B1 B1B1 B1 B1																													
		10																													
24.	<p>a)</p> <table border="1"> <thead> <tr> <th>Age (years)</th> <th>x</th> <th>F</th> <th>xf</th> </tr> </thead> <tbody> <tr> <td>0-5</td> <td>2.5</td> <td>14</td> <td>35</td> </tr> <tr> <td>5-15</td> <td>10</td> <td>41</td> <td>410</td> </tr> <tr> <td>15-25</td> <td>20</td> <td>59</td> <td>1180</td> </tr> <tr> <td>25-45</td> <td>35</td> <td>70</td> <td>2450</td> </tr> <tr> <td>45-75</td> <td>60</td> <td>15</td> <td>900</td> </tr> <tr> <td></td> <td></td> <td>$\sum f = 199$</td> <td>$\sum fx = 4975$</td> </tr> </tbody> </table>	Age (years)	x	F	xf	0-5	2.5	14	35	5-15	10	41	410	15-25	20	59	1180	25-45	35	70	2450	45-75	60	15	900			$\sum f = 199$	$\sum fx = 4975$	B1 B1 M1 A1	
Age (years)	x	F	xf																												
0-5	2.5	14	35																												
5-15	10	41	410																												
15-25	20	59	1180																												
25-45	35	70	2450																												
45-75	60	15	900																												
		$\sum f = 199$	$\sum fx = 4975$																												
	$Mean(\bar{x}) = \frac{\sum fx}{\sum f} = \frac{4975}{199} = 25 \text{ yrs}$																														
	i)																														
		B1 B1 B1B1	Frequency density Age (years) Scale																												

		B1	Correct height Correct internals of the bars.