

MATHEMATICS PAPER 2

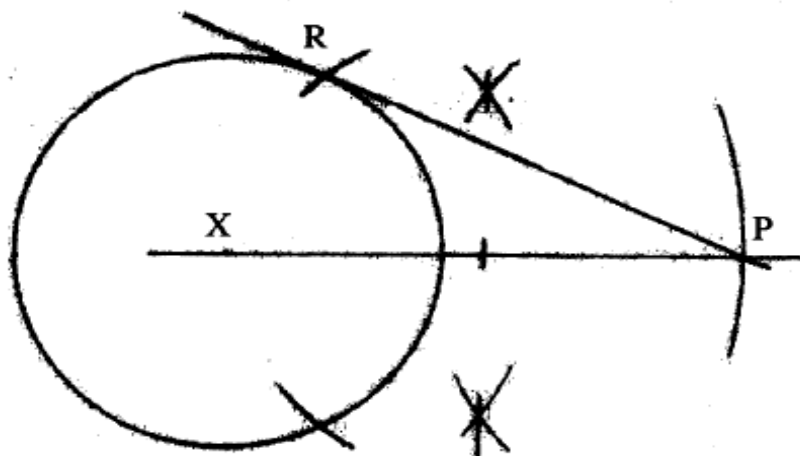
KCSE 2012

ANSWERS

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1.	$\frac{5 \log 4 - 4 \log 5}{\frac{1}{5} \log 4 + \frac{1}{4} \log 5}$ $= \frac{3.010299957 - 2.795880017}{0.120411998 + 0.174742501}$ $= 0.726466785$ $\simeq 07265 \quad (4 \text{ s.f.})$	M1	
		A1	
		2	
2.	$\left(\frac{r}{p}\right)^2 = \frac{m^2}{n-1}$ $n-1 = \left(\frac{mp}{r}\right)^2$ $n = \left(\frac{mp}{r}\right)^2 + 1$	M1	squaring
		M1	
		A1	
		3	
3.	Fraction filled by inlet tap in $1h = \frac{1}{6}$ Fraction filled when two taps open in $1h = \frac{1}{10}$ $\therefore$ fraction emptied by outlet tap in $1h = \frac{1}{6} - \frac{1}{10}$ $= \frac{1}{15}$ Time for outlet tap to empty tank = 15h	B1	for $\frac{1}{6}$ or $\frac{1}{10}$
		M1	
		A1	
		3	
4.	$\underline{R} = 6\underline{i} - 9\underline{j} + 3\underline{k} + 6\underline{i} - 8\underline{j} - 6\underline{k}$ $= 12\underline{i} - 17\underline{j} - 3\underline{k}$ $ \underline{R} = \sqrt{12^2 + 17^2 + 3^2}$ $= \sqrt{442}$ $= 21.02 \simeq 21 \quad (2 \text{ s.f.})$	B1	
		M1	
		A1	
		3	
5.	$\sin(2t + 10)^\circ = 0.5$ $2t + 10 = 30^\circ, 150^\circ$ $t = 10^\circ, 70^\circ$	B1	
		B1	
		2	

6.



Drawing circle

Fixing point P

Bisecting XP and drawing tangent

RP = $5.4 \pm 0.1\text{cm}$

B1

B1

B1

B1

4

7. Amount for Kago

$$= 30000 + \frac{12}{100} \times 30000 \times 5$$

$$= 48000$$

Compound interest rate for Nekesa

$$30000\left(1 + \frac{r}{100}\right)^5 = 48000$$

$$\left(1 + \frac{r}{100}\right)^5 = \frac{48000}{30000} = 1.6$$

$$1 + \frac{r}{100} = \sqrt[5]{1.6}$$

$$r = 100(1.098560543 - 1)$$

$$= 9.9\%$$

B1

M1

M1

A1

4

8. Differences from assumed mean

$$-6 - 2 + 0 + 2 + 3 + 6 + 9 - 5 + 6 + 3 + 9$$

$$-2 + 3 - 6 - 2 + 3 + 2 + 0 + 6 + 9 = 38$$

$$\therefore \text{mean} = 96 + \frac{38}{20}$$

$$= 97.9$$

M1

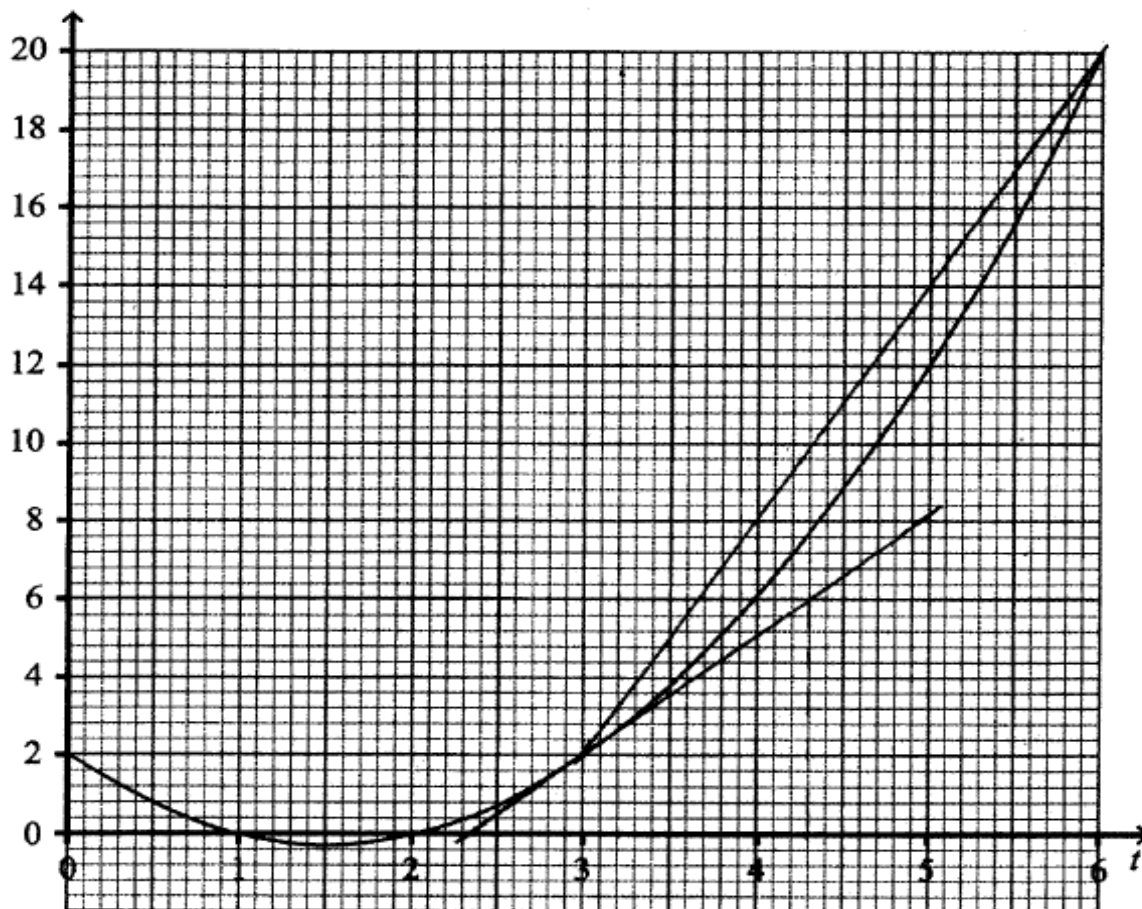
M1

A1

3

differences from the assumed mean

9. $x + y = 17 \dots\dots\dots (i)$ $xy - 5x = 32 \dots\dots (ii)$ from (i) $y = 17 - x$ substituting $y = 17 - x$ in (ii) $x(17 - x) - 5x = 32$ $17x - x^2 - 5x = 32$ $x^2 - 12x + 32 = 0$ $(x - 4)(x - 8) = 0$ $x = 4$ or $x = 8$ substituting $x = 4$ in (i) $4 + y = 17 \Rightarrow y = 13$ substituting $x = 8$ in (ii) $8 + y = 17 \Rightarrow y = 9$	M1 M1 A1 B1 4	for substitution or elimination for both 4 and 8 for both 13 and 9
10. $\frac{\sqrt{5}}{\sqrt{5} - 2} = \frac{\sqrt{5}}{\sqrt{5} - 2} \times \frac{\sqrt{5} + 2}{\sqrt{5} + 2}$ $= \frac{5 + 2\sqrt{5}}{5 - 4}$ $= 5 + 2\sqrt{5}$	M1 A1 2	
11. minimum possible area $= \frac{1}{2}(6.35 \times 3.45)$ $= 10.95375 \text{ cm}^2$ maximum possible area $= \frac{1}{2} \times 6.45 \times 3.55$ $= 11.44875 \text{ cm}^2$ maximum absolute error in area $= \frac{11.44875 - 10.95375}{2}$ $= 0.2475 \text{ cm}^2$	M1 M1 A1 3	for both expressions - min. and max. areas
12. (a) $(1 + x)^7 = 1^7 + 7 \times 1^6 \times x + 21 \times 1^5 \times x^2 + 35 \times 1^4 \times x^3 + \dots$ $= 1 + 7x + 21x^2 + 35x^3$ (b) $(0.94)^7 = [1 + (-0.06)]^7$ $= 1 + 7 \times (-0.06) + 21 \times (-0.06)^2 + 35 \times (-0.06)^3$ $= 1 - 0.42 + 0.0756 - 0.00756$ $= 0.64804$	B1 M1 A1 3	



- (a) Average rate of change between $t = 3$ and $t = 6$

$$\frac{20 - 2}{6 - 3}$$

$$= \frac{18}{3} = 6$$

- (b) Gradient at $t = 3$ seconds

$$\frac{6 - 0}{4.3 - 2.3} = \frac{6}{2}$$

$$= 3 \pm 0.1$$

M1

A1

M1

or equivalent

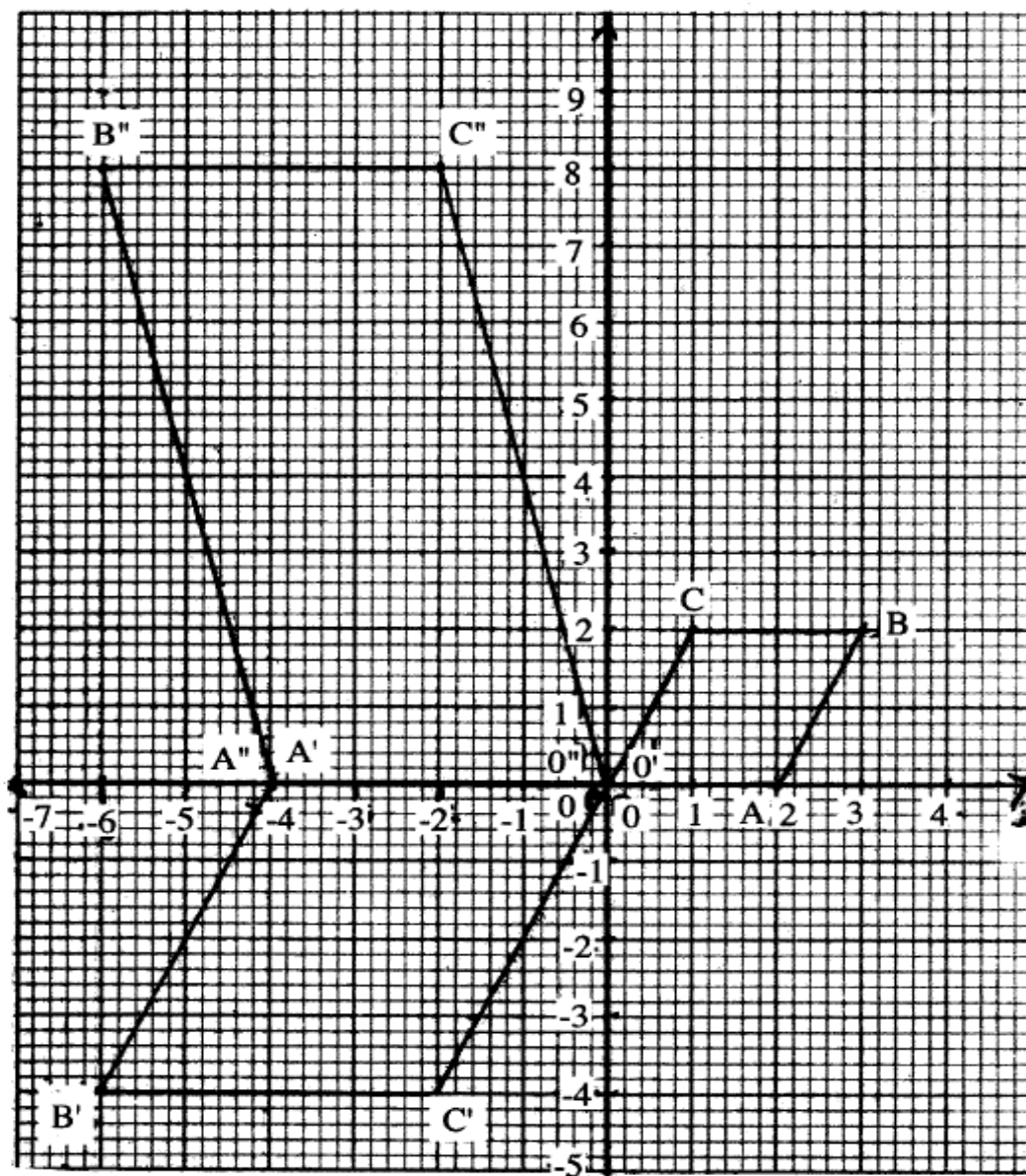
A1

4

14.	(a) Let UV be x cm: $VT \times UT = ST^2$ $(x + 8)8 = 12^2$ $8x = 144 - 64$ $= 80$ $x = 10 \text{ cm}$ (b) $VX = \frac{2}{5} \times 10 = 4 \text{ cm}$ $XU = 10 - 4 = 6 \text{ cm}$ $SX \times XW = VX \times XU$ $SX \times 3 = 4 \times 6$ $SX = 8 \text{ cm}$	M1 A1 M1 A1	
15.	$P \propto \frac{Q}{\sqrt{R}} \Rightarrow P = \frac{kQ}{\sqrt{R}}$ $8 = \frac{k \times 10}{\sqrt{16}}$ $k = 3.2$ $P = \frac{3.2Q}{\sqrt{R}}$	M1 A1 B1	
16.	$OC = \frac{\sqrt{24^2 + 10^2}}{2}$ $= 13$ $\angle VCO = \cos^{-1} \frac{13}{26}$ $= 60^\circ$	M1 M1 A1	

17.	(a) (i) $180000 + (11 - 1)x = 288000$ $10x = 108000$ $x = 10800$ (a) (ii) $S_{11} = \frac{11}{2}(180000 + 288000)$ $= 2574000$ (b) $\frac{150000 \times 1.1^{10}}{12}$ $= 32422$ (c) (i) $\frac{[150000 \times (1.1^{11} - 1)]}{(1.1 - 1)}$ $= 2779675$ (c) (ii) Difference between monthly averages for the 11 years $\frac{2779675 - 2574000}{11 \times 12}$ $= 1558$	M1 A1 M1 A1 M1 A1 M1 A1 M1 A1 10	
18.	(a) $\begin{matrix} & O & A & B & C \\ \begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix} & \begin{pmatrix} 0 & 2 & 3 & 1 \\ 0 & 0 & 2 & 2 \end{pmatrix} & = & \begin{pmatrix} 0 & -4 & -6 & -2 \\ 0 & 0 & -4 & -4 \end{pmatrix} \end{matrix}$ co-ordinates of O'A'B'C' O' (0, 0), A' (-4, 0), B' (-6, -4), C' (-2, -4)	M1 A1	

18. continued



B1 OABC ✓ drawn
 B1 O'A'B'C' ✓ drawn
 B1 O''A''B''C'' ✓ drawn

(b)

$$\begin{pmatrix} 1 & 0 \\ 0 & -2 \end{pmatrix} \begin{pmatrix} 0 & -4 & -6 & -2 \\ 0 & 0 & -4 & -4 \end{pmatrix} = \begin{pmatrix} O' & A' & B' & C' \\ 0 & -4 & -6 & -2 \\ 0 & 0 & 8 & 8 \end{pmatrix}$$

M1

A1

(c)

$$\begin{pmatrix} 1 & 0 \\ 0 & -2 \end{pmatrix} \begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix} = \begin{pmatrix} -2 & 0 \\ 0 & 4 \end{pmatrix}$$

M1

or equivalent

M1

$$\text{inverse } \frac{1}{-8} \begin{pmatrix} 4 & 0 \\ 0 & -2 \end{pmatrix}$$

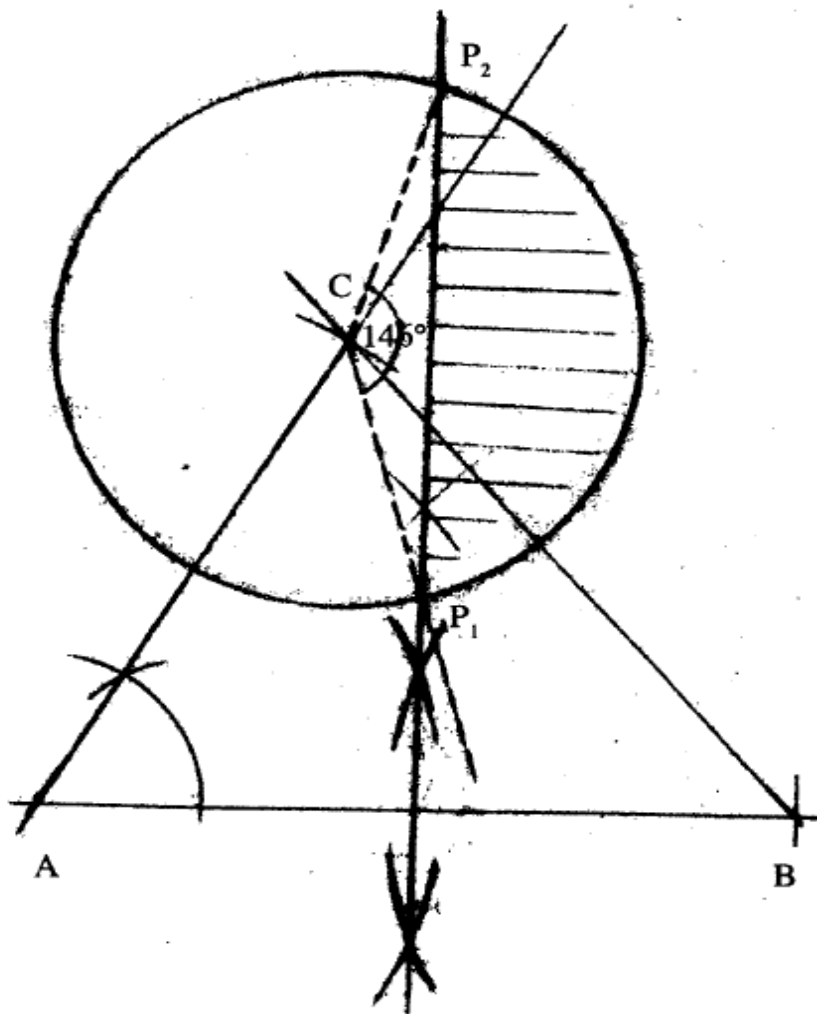
$$= \begin{pmatrix} -\frac{1}{2} & 0 \\ 0 & \frac{1}{4} \end{pmatrix}$$

A1

10

19. (a) (i) $\underline{PN} = \frac{5}{6}\underline{q} - \underline{p}$ (ii) $\underline{QM} = \frac{2}{5}\underline{p} - \underline{q}$ (b) (i) $\underline{OX} = \underline{p} + k\left(\frac{5}{6}\underline{q} - \underline{p}\right)$ $\underline{OX} = \underline{q} + r\left(\frac{2}{5}\underline{p} - \underline{q}\right)$ (ii) $\underline{p} + k\left(\frac{5}{6}\underline{q} - \underline{p}\right) = \underline{q} + r\left(\frac{2}{5}\underline{p} - \underline{q}\right)$ $\underline{p}(1 - k) + \frac{5}{6}k\underline{q} = \underline{q}(1 - r) + \frac{2}{5}r\underline{p}$ $1 - k = \frac{2}{5}r \text{ and } 1 - r = \frac{5}{6}k$ $1 - r = \frac{5}{6}\left(1 - \frac{2}{5}r\right)$ $1 - r = \frac{5}{6} - \frac{1}{3}r$ $\frac{1}{6} = \frac{2}{3}r \Rightarrow r = \frac{1}{4}$ $k = 1 - \frac{2}{5}r \Rightarrow k = 1 - \frac{2}{5} \times \frac{1}{4} = \frac{9}{10}$ (iii) $\underline{QX} = \frac{1}{4}\underline{QM}$ $\underline{MX} = \frac{3}{4}\underline{QM}$ $\therefore \underline{MX} : \underline{XQ} = \frac{3}{4} : \frac{1}{4} = 3 : 1$	B1	
	B1	
	B1	
	B1	
	M1	
$1 - k = \frac{2}{5}r \text{ and } 1 - r = \frac{5}{6}k$	M1	
$1 - r = \frac{5}{6}\left(1 - \frac{2}{5}r\right)$	M1	
$1 - r = \frac{5}{6} - \frac{1}{3}r$		
$\frac{1}{6} = \frac{2}{3}r \Rightarrow r = \frac{1}{4}$		
$k = 1 - \frac{2}{5}r \Rightarrow k = 1 - \frac{2}{5} \times \frac{1}{4} = \frac{9}{10}$	A1	for both values of r and k
(iii) $\underline{QX} = \frac{1}{4}\underline{QM}$	M1	
$\underline{MX} = \frac{3}{4}\underline{QM}$		
$\therefore \underline{MX} : \underline{XQ} = \frac{3}{4} : \frac{1}{4} = 3 : 1$	A1	
	10	

20.	(a) (i) July basic salary		
	$= 17000 \times 1.02$	M1	
	$= 17340$	A1	
	(ii) Total taxable income		
	$= 17340 + 6000 + 2500 + 1800$	M1	
	$= 27640$	A1	
	(b) Gross tax		
	1 st bracket: $9680 \times 10\% = 968$	M1	
	2 nd bracket: $(18800 - 9680) \times 15\% = 1368$	M1	
	3 rd bracket: $(27640 - 18800) \times 20\% = 1768$	M1	$[27649 - (9680 + 9120)]20\%$
	Gross tax: $968 + 1368 + 1768$	M1	
	$= 4104$	A1	
	Net tax: $4104 - 1056 = 3048$	B1	
		10	

B1 construction of 60° B1 completion of Δ

- (a) locus of P
locus of Q

- (b) (i) shading region R

(ii) area of shaded region
area of minor sector P_1CP_2

$$= \frac{146}{360} \times \pi \times 3.5^2$$

$$\simeq 15.6 \text{ cm}^2$$

area of ΔP_1CP_2

$$\frac{1}{2} \times 3.5^2 \sin 146^\circ$$

$$\simeq 3.4 \text{ cm}^2$$

$\therefore$ shaded area

$$15.6 - 3.4$$

$$= 12.2 \text{ cm}^2$$

B1

B1

B2

M1 ($\angle P_1CP_2 = 146^\circ \pm 1^\circ$)

M1

M1

A1

10

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23.	(a) (i) $P(\text{brown}) = \frac{3}{27}$ (ii) $P(\text{pink or white})$ $= \frac{9}{27} + \frac{15}{27}$ $= \frac{8}{9}$ (b) (i) $P(\text{white and brown})$ $= \frac{15}{27} \times \frac{3}{26} + \frac{3}{27} \times \frac{15}{26}$ $= \frac{5}{78} + \frac{5}{78} = \frac{5}{39}$ (ii) white, white + pink, pink + brown, brown $= \frac{15}{27} \times \frac{14}{26} + \frac{9}{27} \times \frac{8}{26} + \frac{3}{27} \times \frac{2}{26}$ $= \frac{35}{117} + \frac{4}{39} + \frac{1}{117} = \frac{16}{39}$	B1 M1 A1 M1 M1 A1 M1 M1 M1 A1 10	
24.	(a) (i) $\frac{dv}{dt} = 4 - t$ $V = \int (4 - t) dt$ $= 4t - \frac{1}{2}t^2 + c$ when $t = 0, v = 3 \text{ m/s}$ $\therefore 3 = 4 \times 0 - \frac{1}{2} \times 0^2 + c$ $3 = c$ $\therefore V = 4t - \frac{1}{2}t^2 + 3$ (ii) when $t = 2$ seconds $V = 4 \times 2 - \frac{1}{2} \times 2^2 + 3$ $= 8 - 2 + 3$ $= 9 \text{ m/s}$ (b) (i) At maximum velocity $\frac{dv}{dt} = 0$ i.e. $4 - t = 0$ $t = 4$ seconds (ii) $\int_0^4 4t - \frac{1}{2}t^2 + 3 = \frac{4}{2}t^2 - \frac{1}{2} \times \frac{1}{3}t^3 + 3t \Big _0^4$ $= 2t^2 - \frac{1}{6}t^3 + 3t \Big _0^4$ $= [2 \times 16 - \frac{1}{6} \times 64 + 12] - 0$ $= 32 - 10\frac{2}{3} + 12 = 33\frac{1}{3}$	B1 B1 B1 M1 A1 M1 A1 M1 M1 A1 10	