## THE KENYA NATIONAL EXAMINATIONS COUNCIL Kenya Certificate of Secondary Education



## 121/2

# MATHEMATICS ALT A

# Paper 2

Nov. 2017 - 2½ hours

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Candidate's Signature				1
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Instructions to candidates		And the State of t		
<ul><li>(a) Write your name and index number in th</li><li>(b) Sign and write the date of examination in</li></ul>	ne spaces pro in the spaces	vided above.		and the second

- (c) This paper consists of **two** sections: **Section I** and **Section II**.
- (d) Answer all the questions in Section I and only five questions from Section II.
- (e) Show all the steps in your calculations, giving your answers at each stage in the spaces provided below each question.
- Marks may be given for correct working even if the answer is wrong.
- (g) Non-programmable silent electronic calculators and KNEC Mathematical tables may be used, except where stated otherwise.
- (h) This paper consists of 20 printed pages.
- (i) Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.
- Candidates should answer the questions in English.

#### For Examiner's Use Only Section I

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Total
				i												

#### Section II

17	18	19	20	21	22	23	24	Total

Grand	
Total	





### SECTION I (50 marks)

Answer all the questions in this section in the spaces provided.

1. The roots of a quadratic equation are  $x = \frac{-3}{5}$  and x = 1. Form the quadratic equation in the form  $ax^2 + bx + c = 0$  where a, b and c are integers. (2 marks)

A tailor intended to subdivide a piece of cloth into 7 equal parts. She approximated  $\frac{1}{7}$  m to 0.14 m. Calculate the percentage error in the approximation. (3 marks)

3. A miller was contracted to make porridge flour to support a feeding program. He mixed millet, sorghum, maize and Omena in the ration 1:2:5:1. The cost per kilogram of millet was Ksh 90, sorghum Ksh 120, maize Ksh 30 and omena Ksh 150.

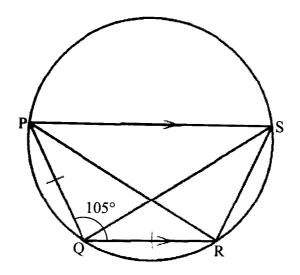
Calculate:

(a) the cost of one kilogram of the mixture;

(2 marks)

(b) the selling price of 1 kg of the mixture if the miller made a 30% profit.

- 4. Without using mathematical tables or a calculator, evaluate  $\frac{5}{6} \log_{10} 64 + \log_{10} 50 4\log_{10} 2$ . (3 marks)
- 5. In the figure below, PQRS is a cyclic quadrilateral. PQ = QR,  $\angle PQR = 105^{\circ}$  and PS is parallel to QR.



Determine the size of:

(a) ∠ PSR;

(1 mark)

(b)  $\angle PQS$ .

6. Make t the subject of 
$$s = \sqrt{\frac{3d(t-d)}{8}}$$
.

(3 marks)

7. Simplify 
$$\frac{3}{3-\sqrt{7}}$$
.

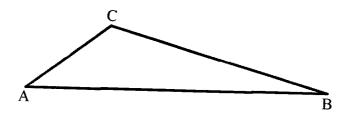
(2 marks)

- 8. Using a ruler and a pair of compasses only, construct:
  - (a) a triangle LMN in which LM = 5 cm, LN = 5.6 cm and  $\angle$  MLN =  $45^{\circ}$ .

(2 marks)

(b) the circle that touches all the sides of the triangle.

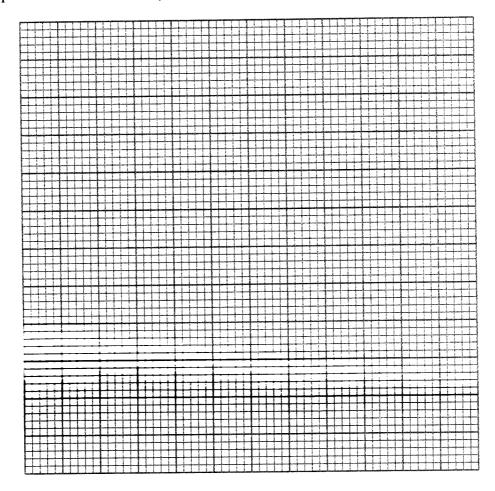
**9.** The figure below is a triangle ABC.



- (a) On the triangle, locate the locus of points equidistant from AC and AB and 5 cm from B. (2 marks)
- (b) Shade the region R, inside the triangle, which is less than 5 cm from B and nearer to AC than AB. (1 mark)
- 10. An aircraft took off from a point P (65° S, 76° W) and flew due North to a point Q. The distance between P and Q is 5 400 nm.

  Determine the position of Q. (3 marks)

11. The equation of a circle is  $x^2 + y^2 - 4x + 6y + 4 = 0$ . On the grid provided, draw the circle.



(4 marks)

12. Determine the amplitude, period and the phase angle of the curve:

(3 marks)

$$y = \frac{5}{2}\sin(4\theta + 60^\circ)$$

13. A basket ball team scored the following points in 6 matches:
10, 12, 14, 16, 28 and 30.
Using an assumed mean of 15. determine the standard deviation correct to 2 decimal places.
(4 marks)

14. A committee of 3 people was chosen at random from a group of 5 men and 6 women. Find the probability that the committee consisted of more men than women. (4 marks)

15. The area of a triangle is 24 square units. The triangle is mapped onto image P by the matrix

 $\begin{pmatrix} 6 & 5 \\ 3 & 4 \end{pmatrix}$ . Find the area of the image P.

(2 marks)

16. Given that OA = 3i + 4j + 7k, OB = 4i + 3j + 9k and OC = i + 6j + 3k,

show that points A, B and C are collinear.

(3 marks)

# **SECTION II** (50 marks)

Answer any five questions from this section in the spaces provided.

17. The income tax rates of a certain year were as shown in the table below:

Monthly taxable income in Kenya shillings(Ksh)	Tax rate percentage(%) in each shilling
0 to 9680	10
9681 to 18800	15
18801 to 27920	20
27921 to 37040	
37041 and above	30

In that year, Shaka's monthly earnings were as follows:

Basic salary House allowance Medical allowance Transport allowance	Ksh 28 600 Ksh 15 000 Ksh 3 200 Ksh 540
	Ksn 540

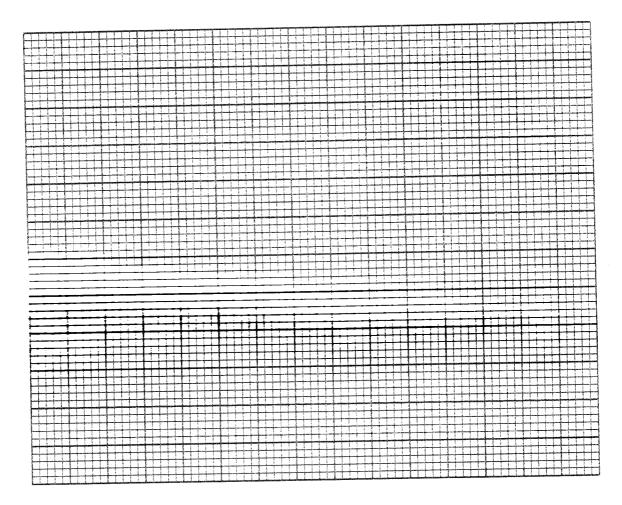
Shaka was entitled to a monthly tax relief of Ksh 1056.

(a) Calculate the tax charged on Shaka's monthly earnings. (6 marks)

(b) Apart from income tax, the following monthly deductions were made; a Health Insurance fund of Ksh 500, Education Insurance of Ksh 1 200 and 2% of his basic salary for widow and children pension scheme. Calculate Shaka's monthly net income from his employment.

(4 marks)

- 18. The vertices of a rectangle ABCD are: A(0,2), B(0,4), C(4,4) and D(4,2). The vertices of its image under a transformation T are; A'(0,2), B'(0,4), C'(8,4) and D'(8,2).
  - (a) On the grid provided, draw the rectangle ABCD and its image A'B'C'D' under T. (2 marks)



(ii)	Describe fully	the transformation	T
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(3 marks)

(iii) Determine the matrix of transformation.

(2 marks)

(b) On the same grid as in (a), draw the image of rectangle ABCD under a shear with line x = -2 invariant and A(0, 2) is mapped onto A"(0,0). (3 marks)

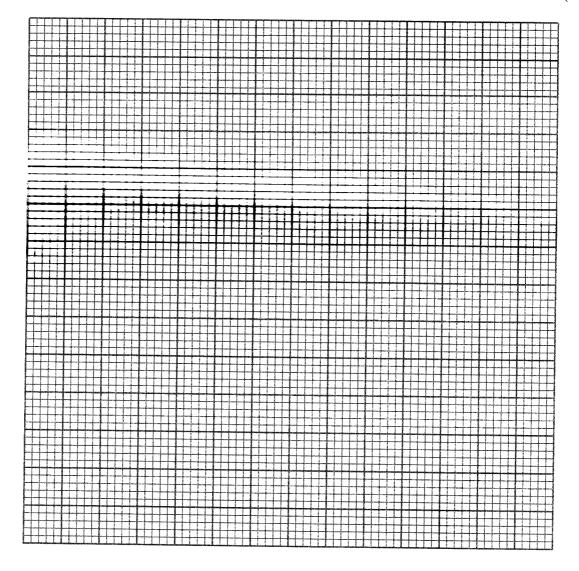
19. (a) The table below shows values of x and some values of y for the curve  $y = x^3 - 2x^2 - 9x + 8$  for  $-3 \le x \le 5$ . Complete the table.

X	-3	-2	-1	0	1	2	3	4	5
$y = x^3 - 2x^2 - 9x + 8$	-10		14	0		-10		4	``

(2 marks)

(b) On the grid provided, draw the graph of  $y = x^3 - 2x^2 - 9x + 8$  for  $-3 \le x \le 5$ . Use the scale; 1 cm represents 1 unit on the x-axis 2 cm represents 10 units on the y-axis

(3 marks)



(c) Use the graph to solve the equation  $x^3 - 2x^2 - 9x + 8 = 0$ .

(1 mark)

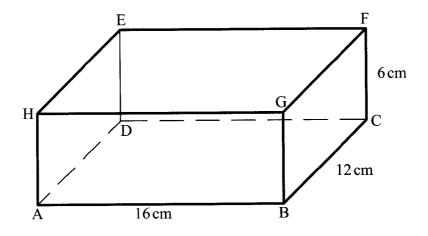
(ii) By drawing a suitable straight line on the graph, solve the equation

$$x^3 - 2x^2 - 11x + 6 = 0.$$

(4 marks)



20. The figure below represents a cuboid ABCDEFGH in which  $AB = 16 \,\mathrm{cm}$ ,  $BC = 12 \,\mathrm{cm}$  and  $CF = 6 \,\mathrm{cm}$ .



(a) Name the projection of the line BE on the plane ABCD.

(1 mark)

- (b) Calculate, correct to 1 decimal place:
  - (i) the size of the angle between AD and BF;

(2 marks)

(ii) the angle between line BE and the plane ABCD;

(3 marks)

(iii) the angle between planes HBCE and BCFG.

(2 marks)

(c) Point N is the midpoint of EF. Calculate the length BN, correct to 1 decimal place.

- 21. Three quantities X, Y and Z are such that X varies directly as the square root of Y and inversely as the fourth root of Z. When X = 64, Y = 16 and Z = 625.
  - (a) Determine the equation connecting X, Y and Z.

(4 marks)

(b) Find the value of Z when Y = 36 and X = 160.

(2 marks)

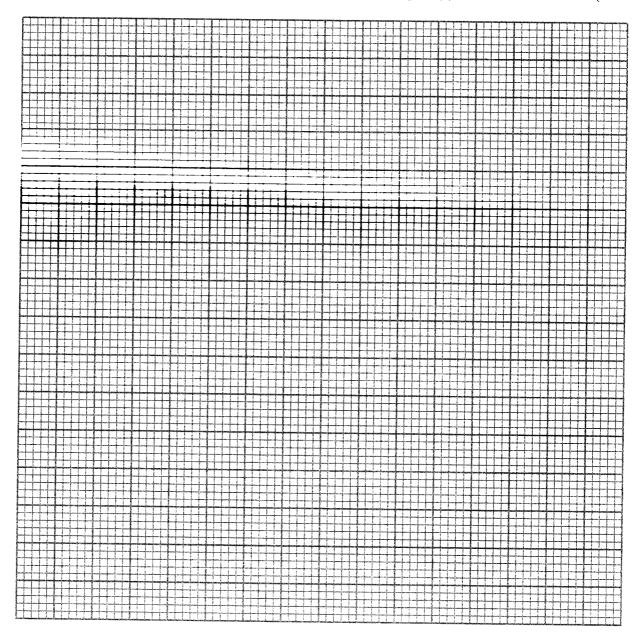
(c) Find the percentage change in X when Y is increased by 44%.

(4 marks)

- 22. A trader stocks two brands of rice A and B. The rice is packed in packets of the same size. The trader intends to order fresh supplies but his store can accommodate a maximum of 500 packets. He orders at least twice as many packets of A as of B. He requires at least 50 packets of B and more than 250 packets of A. If he orders x packets of A and y packets of B,
  - (a) Write the inequalities in terms of x and y which satisfy the above information. (4 marks)

(b) On the grid provided, represent the inequalities in part (a) above.

(4 marks)



(c) The trader makes a profit of Ksh 12 on a packet of type A rice and Ksh 8 on a packet of type B rice. Determine the maximum profit the trader can make. (2 marks)

23.	(a)	The 5th term of an AP is 82 and the 12th term is 103.								
		Find:								
		(i)	the first term and the common difference;	(3 marks)						
		(ii)	the sum of the first 21 terms.	(2 marks)						

(b) A staircase was built such that each subsequent stair has a uniform difference in height. The height of the 6<sup>th</sup> stair from the horizontal floor was 85 cm and the height of the 10<sup>th</sup> stair was 145 cm.

Calculate the height of the 1<sup>st</sup> stair and the uniform difference in height of the stairs.

(3 marks)

(c) During the construction of the staircase, each step was supported by a vertical piece of timber. If the staircase has 11 stairs, calculate the total length of timber used. (2 marks)

The of i	e length of a room is 3 m shorter than three times its width. The height of the room is a quarter its length. The area of the floor is $60 \mathrm{m}^2$ .							
(a)	Ca	lculate the dimensions of the room.	(5 marks)					
(b)	The bord	floor of the room was tiled leaving a border of width $y$ m, all release 1.69 m <sup>2</sup> , find:	ound. If the area of the					
	(i)	the width of the border;	(4 marks)					
	(ii)	the dimensions of the floor area covered by tiles.	(1 mark)					

